

Baryon Asymmetry of the Universe

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§1. Evidence of the **BAU**

Baryon Asymmetry of the Universe

$$\frac{n_B}{s} = \frac{n_b - n_{\bar{b}}}{s} = (0.48 - 0.98) \times 10^{-10}$$

$$s = \frac{\pi^2}{45} g_* T^3 \simeq 7.04 n_\gamma: \text{ entropy density}$$

$g_* = \text{massless degrees of freedom}$

— constant during the expansion of the universe, once $\Delta B \neq 0$ is turned off

$$n_b, n_{\bar{b}} \propto a(t)^{-3} \propto T^3 \text{ [entropy } a^3 s \propto a^3 T^3 = \text{const., where } a = \text{scale factor}]$$

This value is determined by the data of

- ★ WMAP — observation of fluctuation in the Cosmic Microwave Background Radiation

The evolution of the fluctuation is determined by the components of the universe (baryon, CDM, electron, photon) at the decoupling.

$$\longrightarrow T_0, H_0 (\rightarrow \rho_C = 3H_0^2 / (8\pi G)), \Omega_B = \rho_B / \rho_C (\rho = \text{energy density})$$

- ★ Big Bang Nucleosynthesis

- $T \gg 1\text{MeV}$



- $T = T_F \simeq 1\text{MeV}$ ($\Gamma_{n \leftrightarrow p} \simeq H$)

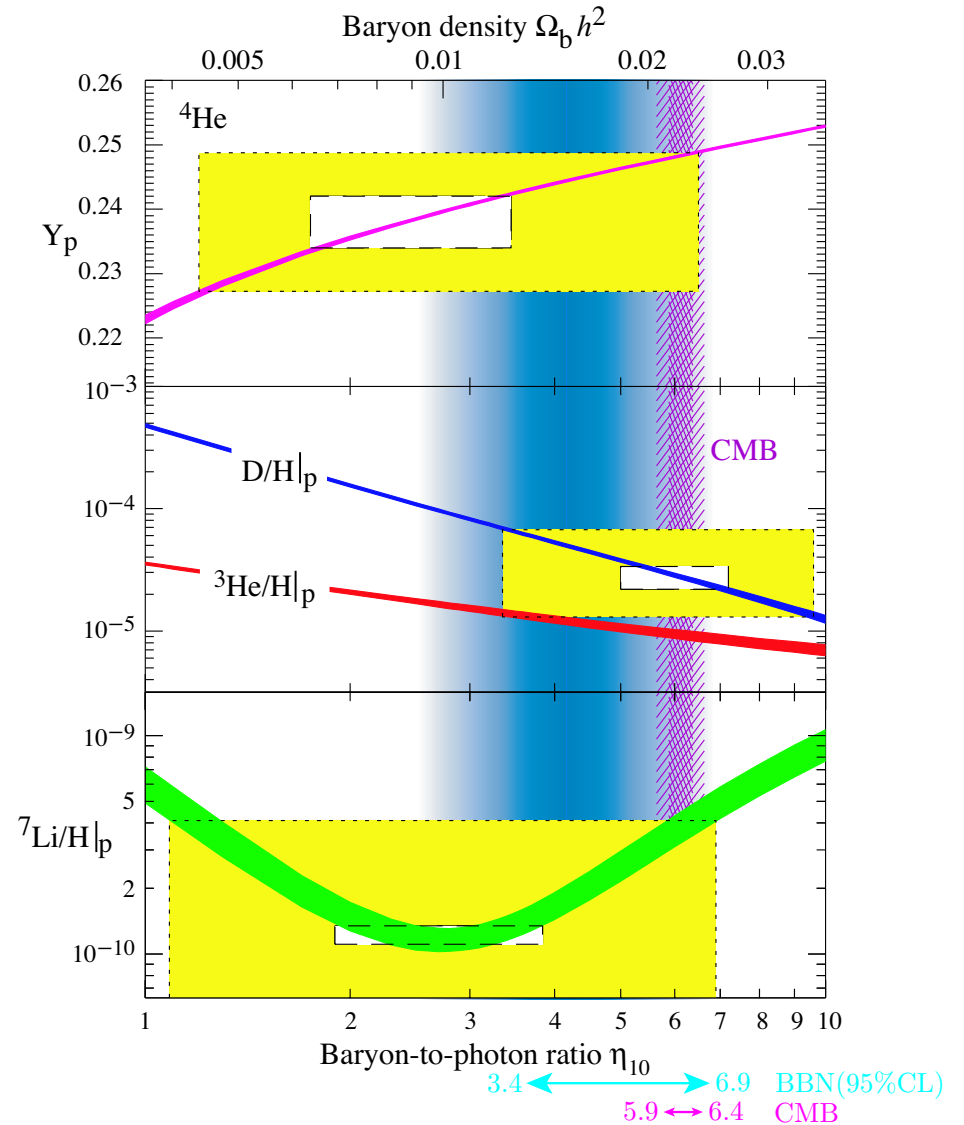
$$\frac{n_n}{n_p} \simeq e^{-(m_n - m_p)/T_F} \simeq \frac{1}{6}$$

- $T = 0.3 - 0.1\text{MeV}$

depending on $\eta = \frac{n_B}{n_\gamma}$, $\frac{n_n}{n_p} = \frac{1}{7} - \frac{1}{6}$

^4He mass fraction

$$Y \equiv \frac{2n_n}{n_n + n_p} \quad \left(= 0.25 \leftrightarrow \frac{n_n}{n_p} = \frac{1}{7} \right)$$



1. observed antiparticles in cosmic rays = **secondary** antiparticles
2. clusters of galaxies are stable

mass of a cluster: $M_{\text{cluster}} \simeq 10^{12-14} M_{\odot}$ (M_{\odot} =solar mass)

In the universe, is there **net baryon number**?

Starting from a **Baryon-symmetric universe**, can we extract finite n_B ?

At $T < 1\text{GeV}$, *a bit of* nucleons and anti-nucleons exist with the same number

because of **thermal fluctuation**: $n_N = n_{\bar{N}} = (m_N T)^{3/2} e^{-m_N/T}$

$$\frac{n_b}{s} = \frac{n_{\bar{b}}}{s} \simeq 8 \times 10^{-11} \quad \text{at } T = 38\text{MeV}$$

At this T , **total energy within a causal volume** ($\sim H^{-3}$) is $10^{-7} M_{\odot} \ll 10^{12} M_{\odot}$

At a higher T , there are more n_b/s and $n_{\bar{b}}/s$, but

$$E_{\text{causal}} \sim \rho(T) H^{-3}(T) \sim T^4 (T^2/m_{\text{Pl}})^{-3} = m_{\text{Pl}}^3 T^{-2} < 10^{-7} M_{\odot},$$

where

$$H = \frac{\dot{a}(t)}{a(t)} = \sqrt{\frac{8\pi G}{3} \rho(T)} \quad \text{with} \quad \rho(T) = g_* \frac{\pi^2}{30} T^4$$

Even the *Maxwell's demon* could not separate matter and antimatter to create the present universe, without violating causality.

Before the era of nucleosynthesis, we must have

$$\frac{n_B}{s} = (0.48 - 0.98) \times 10^{-10}$$

over a region broader than a causal region at $T = 1\text{MeV}$.

§2. Requirements for the **baryogenesis**

= generating B starting from B -symmetric universe

Sakharov's 3 conditions

- (1) **Baryon number violating process**
- (2) **Violation of C and CP symmetries**
- (3) **Out of equilibrium**

(1) is obvious.

(3) In equilibrium, $\Delta B \neq 0$ -process and its inverse occur with the same probability. Then no B is generated.

Let us consider the case in which (2) is not satisfied.

Suppose that a local state of the spatially uniform universe is described by

density operator

$$\rho(t) = \sum_n p_n |n(t)\rangle \langle n(t)| \quad (p_n = \text{prob. to find the universe in the state } |n(t)\rangle)$$

Expectation value of some observable \mathcal{O} :

$$\langle \mathcal{O} \rangle(t) = \text{Tr} [\rho(t) \mathcal{O}] = \sum_n p_n \langle n(t) | \mathcal{O} | n(t) \rangle$$

time evolution of $\rho(t)$ is governed by the Liouville equation:

$$i\hbar \frac{\partial \rho(t)}{\partial t} + [\rho(t), H] = 0$$

$$(\Leftarrow \text{Schrödinger eq. } i\hbar \frac{\partial}{\partial t} |n(t)\rangle = H |n(t)\rangle)$$

ρ_0 : density operator of an initial state with $n_B = 0$ $\langle n_B \rangle_0 \equiv \text{Tr} [\rho_0 n_B] = 0$

density operator $\rho(t)$ at a later time is given by the solution to

$$i\hbar \frac{\partial \rho(t)}{\partial t} + [\rho(t), H] = 0$$

with the initial condition $\rho(t_0) = \rho_0$

The solution is formally written in terms of H and ρ_0

\Rightarrow If H is invariant under C - or CP -trf. $\implies [\rho, C] = 0$ or $[\rho, CP] = 0$

$CBC^{-1} = -B$, $CPB(CP)^{-1} = -B$ (i.e., B is vectorlike and odd under C)

$$\Rightarrow \left\{ \begin{array}{l} \langle n_B \rangle = \text{Tr}[\rho n_B] = \text{Tr}[\rho C n_B C^{-1}] = -\text{Tr}[\rho n_B] = 0 \\ \text{or} \\ \langle n_B \rangle = \text{Tr}[\rho CP n_B (CP)^{-1}] = -\text{Tr}[\rho n_B] = 0 \end{array} \right.$$

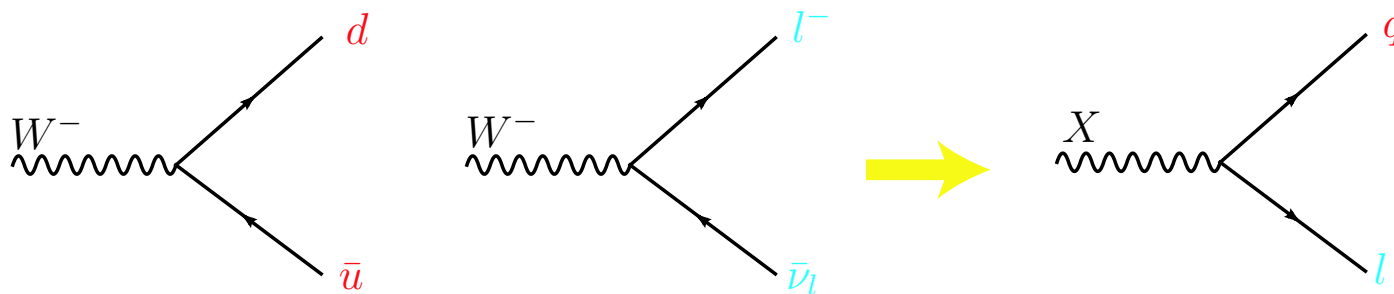
\therefore **Both C and CP must be violated to have $\langle n_B \rangle \neq 0$**

§3. Scenarios of baryogenesis

— models of particle physics realizing baryogenesis

(1) $\Delta B \neq 0$ process

- quark-lepton mixing — in Grand Unified Theories (GUTs)



- in Supersymmetric theories,

$$\left. \begin{array}{l} \text{quark: } q \leftrightarrow \tilde{q} \text{ : scalar quark (squark)} \\ \text{lepton: } l \leftrightarrow \tilde{l} \text{ : scalar lepton (slepton)} \end{array} \right\} \implies \langle \tilde{q} \rangle \neq 0, \langle \tilde{l} \rangle \neq 0$$

- axial $U(1)$ anomaly in the $(B + L)$ -current
— exists in the Standard Model

$$\partial_\mu j_{B+L}^\mu = \frac{N_f}{16\pi^2} [g_2^2 \text{Tr}(F_{\mu\nu} \tilde{F}^{\mu\nu}) - g_1^2 B_{\mu\nu} \tilde{B}^{\mu\nu}] \neq 0$$

for *some specific configuration* of the $SU(2)$ -gauge field

We shall discuss this process later.

All these processes must be **suppressed at $T = 0$** , in order **for a proton not to decay**

⇒

- in GUTs, m_X must be heavier than some value $\sim 10^{16} \text{GeV}$
- The potential for the squark fields must have such a form that $\langle \tilde{q} \rangle \neq 0$ is realized in the early universe, while $\langle \tilde{q} \rangle = 0$ at $T = 0$
- at $T = 0$, $\Delta(B + L) \neq 0$ process occurs by quantum tunneling
As shown later, the probability is negligible

(2) C and CP violation

★ C violation ← **chiral** gauge interactions in EW theory and GUTs

$SU(2)_L$ gauge int., different $U(1)_Y$ charges for L - and R -fermions

★ CP violation ← **complex parameters** with irreducible phases

In renormalizable field theories, only some types of interactions can violate CP .

● In the SM, **KM phase** and $F_{\mu\nu}\tilde{F}^{\mu\nu}$ (θ -term)

$|\theta_{\text{QCD}}| \simeq 0$ by neutron EDM experiment

● Extended models:

▷ SUSY models: relative phases of μ , gaugino mass, A , B (soft-SUSY-br.)

▷ extended Higgs sector: **complex Higgs self-couplings**

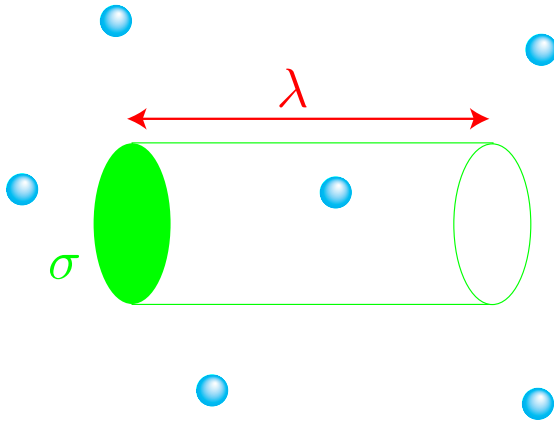
magnitude of CP violation is limited by experiments

— e.g., B-factory, EDM of neutron and lepton, K-rare processes

(3) Out of equilibrium

“equilibrium in the expanding universe” \Leftrightarrow time scale of process: $\tau < H(T)^{-1}$

for relativistic particles, $\tau \simeq \lambda$: mean free path



σ : total cross section

$n(T)$: particle number density

$$\sigma \cdot \lambda = \frac{1}{n(T)}$$

$$H(T) = \sqrt{\frac{8\pi G}{3} \rho(T)} \simeq 1.66 \sqrt{g_*} \frac{T^2}{m_{\text{Pl}}}$$

$$\rho(T) = \frac{\pi^2}{30} g_* T^4$$

relativistic degrees of freedom for SM with N_f generation, N_H Higgs doublets

$$g_* = 24 + 4N_H + \frac{7}{8} \cdot 30N_f \stackrel{\text{MSM}}{=} 106.75$$

number density: $n(T) = g \int \frac{d^3\mathbf{k}}{(2\pi)^3} \frac{1}{e^{\sqrt{k^2+m^2}/T} \mp 1} \stackrel{m \ll T}{\simeq} g \begin{cases} \frac{\zeta(3)}{\pi^2} T^3 \\ \frac{3}{4} \frac{\zeta(3)}{\pi^2} T^3 \end{cases}$

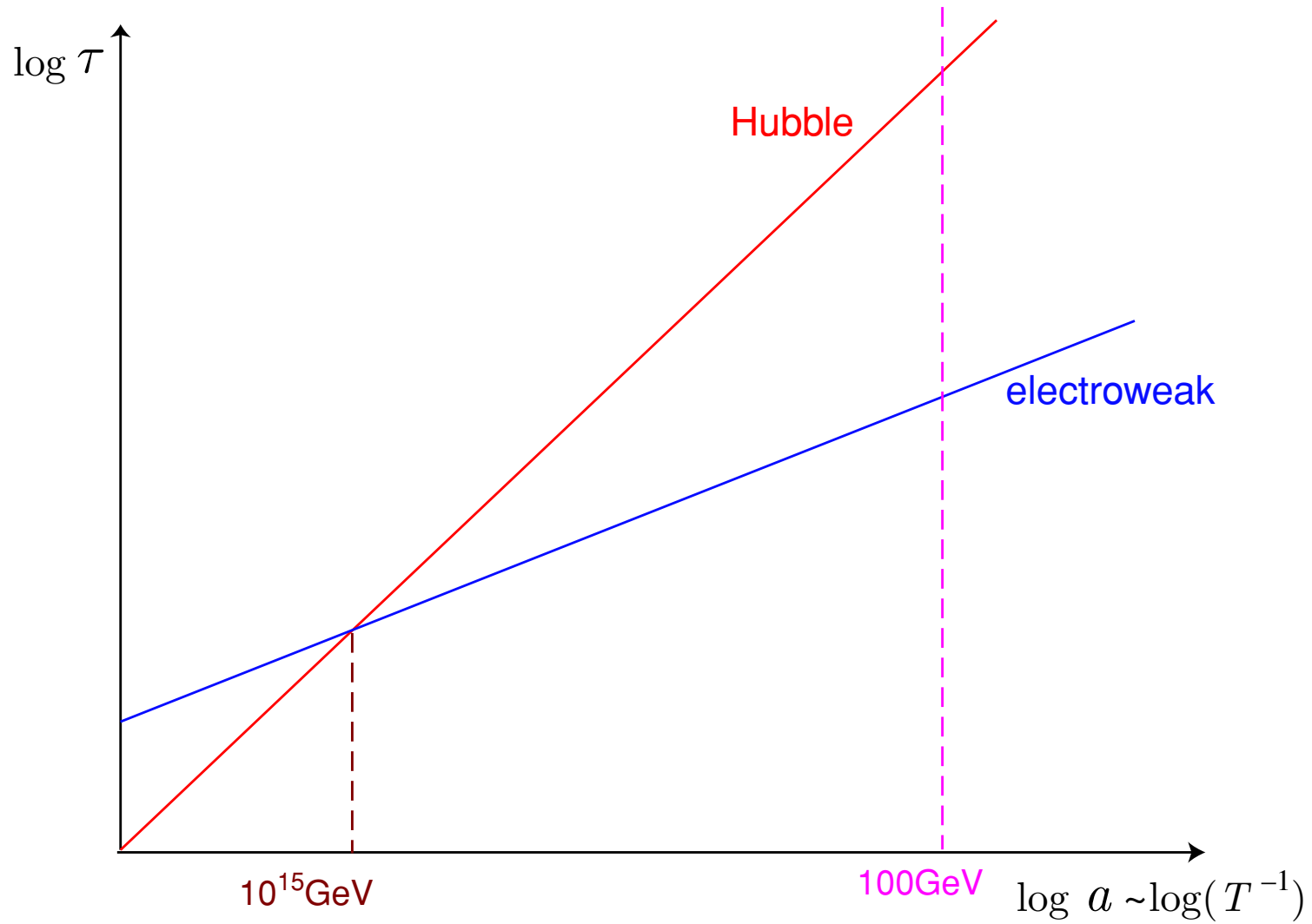
$\zeta(3) = 1.2020569 \dots$

for relativistic particles, $\sigma \simeq \frac{\alpha^2}{s} \simeq \frac{\alpha^2}{T^2} \quad \therefore \quad \lambda \simeq \frac{10}{gT^3} \left(\frac{\alpha^2}{T^2} \right)^{-1} = \frac{10}{g\alpha^2 T}$

$T = 100\text{GeV}$:

{	$H(T)^{-1} \simeq 10^{14} \text{ GeV}^{-1}$	expansion
	$\lambda_s \simeq \frac{1}{\alpha_s^2 T} \sim 1 \text{ GeV}^{-1}$	strong interactions
	$\lambda_{EW} \simeq \frac{1}{\alpha_W^2 T} \sim 10 \text{ GeV}^{-1}$	EW interactions
	$\lambda_Y \simeq \left(\frac{m_W}{m_f} \right)^4 \lambda_{EW}$	Yukawa interactions

time scale of EW interaction vs that of the expansion



Possible out-of-equilibrium processes

$$\tau_{\text{process}} < H(T) ?$$

- Expansion of the universe

EW or GUTs interaction in the radiation dominated universe at $T > 10^{15} \text{ GeV}$

Heavy particle (e.g., heavy Majorana neutrino) at $T > 10^{10} \text{ GeV}$

- First-order phase transition

some rare process runs out of equil. even at $T = 100 \text{ GeV}$

— $(B + L)$ -violating process in EW theory

- Reheating or preheating after inflation

accompanying production of a large amount of entropy

—> dilution of baryon number density

An example — GUTs

[Yoshimura, Phys. Rev. Lett. 41 ('78)]

minimal $SU(5)$ model:

$$\text{matter: } \begin{cases} \mathbf{5}^* : \psi_L^i & \ni d_R^c, l_L \\ \mathbf{10} : \chi_{[ij]L} & \ni q_L, u_R^c, e_R^c \end{cases} \quad \text{gauge: } A_\mu = \begin{pmatrix} G_\mu, B_\mu & X_\mu^{a\alpha} \\ X_\mu^{a\alpha} & W_\mu, B_\mu \end{pmatrix}$$

$$i = 1 - 5 \rightarrow (\alpha = 1 - 3, a = 1, 2)$$

$$\begin{aligned} \mathcal{L}_{\text{int}} &\ni g \bar{\psi} \gamma^\mu A_\mu \psi + g \text{Tr} [\bar{\chi} \gamma^\mu \{A_\mu, \chi\}] \\ &\ni g X_{\alpha\mu}^a [\varepsilon^{\alpha\beta\gamma} \bar{u}_{R\gamma}^c \gamma^\mu q_{L\beta a} + \epsilon_{ab} (\bar{q}_{Lb}^\alpha \gamma^\mu e_R^c + \bar{l}_{Lb} \gamma^\mu d_R^{c\alpha})] \end{aligned}$$

Expectation value of ΔB in decays of X - \bar{X} pairs generated from the plasma

$$\langle \Delta B \rangle = \frac{2}{3}r - \frac{1}{3}(1-r) - \frac{2}{3}\bar{r} + \frac{1}{3}(1-\bar{r}) = r - \bar{r}$$

$\therefore C$ or CP is conserved ($r = \bar{r}$)

$$\implies \Delta B = 0$$

process	BR	ΔB
$X \longrightarrow qq$	r	$2/3$
$X \longrightarrow \bar{q}\bar{l}$	$1-r$	$-1/3$
$\bar{X} \longrightarrow \bar{q}\bar{q}$	\bar{r}	$-2/3$
$\bar{X} \longrightarrow q, l$	$1-\bar{r}$	$1/3$

If the inverse process is suppressed, $B \propto r - \bar{r}$ is generated.

Indeed, at $T \simeq m_X$, the decay rate of X : $\Gamma_D \simeq \alpha m_X$ ($\alpha \sim 1/40$)

$\Rightarrow \Gamma_D \simeq H(T = m_X) \quad \therefore$ annihilation and production of $X\bar{X}$ out of equil.

$$H(T) \simeq 1.66 \sqrt{g_*} \frac{T^2}{m_{\text{Pl}}}$$

SU(5) GUT conserves $B - L$ — $(B + L)$ -genesis

EW $\Delta(B + L) \neq 0$ process in equilibrium $\rightarrow B + L \rightarrow 0$



new possibility of baryogenesis

$B - L \neq 0$ before EW $\Delta(B + L) \neq 0$ process in equil.

Leptogenesis: $\Delta L \neq 0 \rightarrow B = -L$

EW $\Delta(B + L) \neq 0$ process \Leftarrow chiral $U(1)$ anomaly in $(B + L)$ -current

$$\partial_\mu j_{B+L}^\mu = \frac{N_f}{16\pi^2} [g_2^2 \text{Tr}(F_{\mu\nu} \tilde{F}^{\mu\nu}) - g_1^2 B_{\mu\nu} \tilde{B}^{\mu\nu}]$$

$$\partial_\mu j_{B-L}^\mu = 0$$

$N_f = \#$ of generations

$$\tilde{F}^{\mu\nu} \equiv \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$$

integrating the sum of these eqs.

$$\begin{aligned} B(t_f) - B(t_i) &= \frac{N_f}{32\pi^2} \int_{t_i}^{t_f} d^4x \left[g_2^2 \text{Tr}(F_{\mu\nu} \tilde{F}^{\mu\nu}) - g_1^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \right] \\ &= N_f [N_{CS}(t_f) - N_{CS}(t_i)] \end{aligned}$$

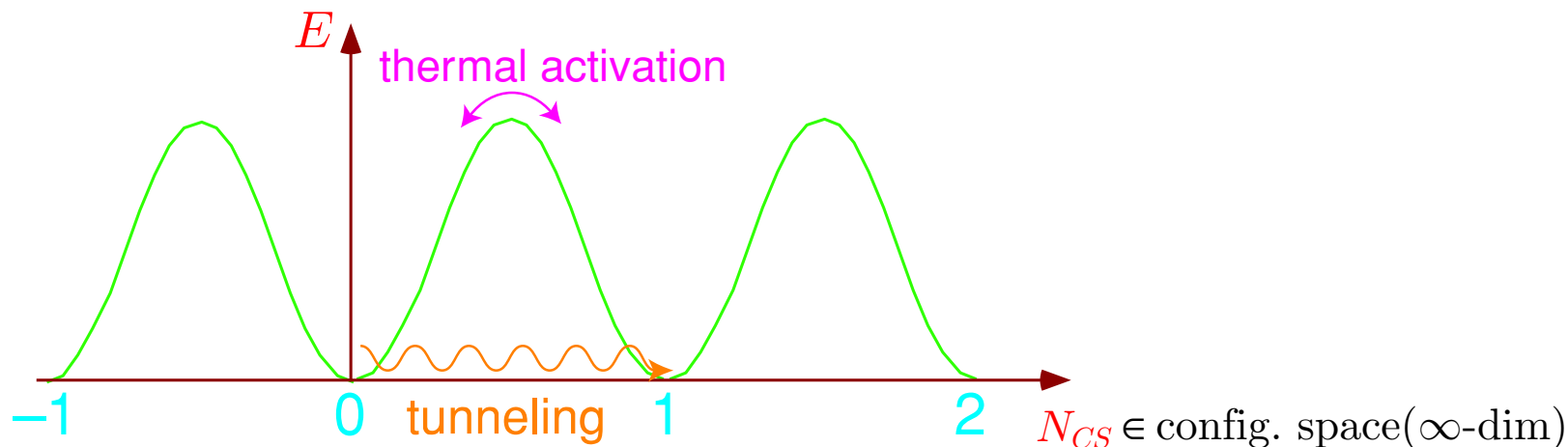
where N_{CS} is the Chern-Simons number: in the $A_0 = 0$ -gauge

$$N_{CS}(t) = \frac{1}{32\pi^2} \int d^3x \epsilon_{ijk} \left[g_2^2 \text{Tr} \left(F_{ij} A_k - \frac{2}{3} g A_i A_j A_k \right) - g_1^2 B_{ij} B_k \right]_t$$

classical vacuum of the gauge fields: $\mathcal{E} = \frac{1}{2}(\mathbf{E}^2 + \mathbf{B}^2) = 0 \iff F_{\mu\nu} = B_{\mu\nu} = 0$

$\iff A = iU^{-1}dU, B = dv$ with $U \in SU(2)$ $U(\mathbf{x}) : S^3 \rightarrow U \in SU(2) \simeq S^3$

$\pi_3(S^3) \simeq \mathbf{Z} \implies U(\mathbf{x})$ is classified by the integer N_{CS}



$\Delta(B + L) \neq 0$ process $\left\{ \begin{array}{ll} \triangleright \text{Quantum Tunneling} & \text{low-}T \\ \triangleright \text{Thermal Activation} & \text{high-}T \end{array} \right.$

tunnel. prob. $\sim e^{-2S_{\text{instanton}}} = e^{-8\pi^2/g_2^2} \simeq e^{-164} \ll 1$

\therefore no proton-decay problem

★ $(B + L)$ -transition (sphaleron transition) rate ★

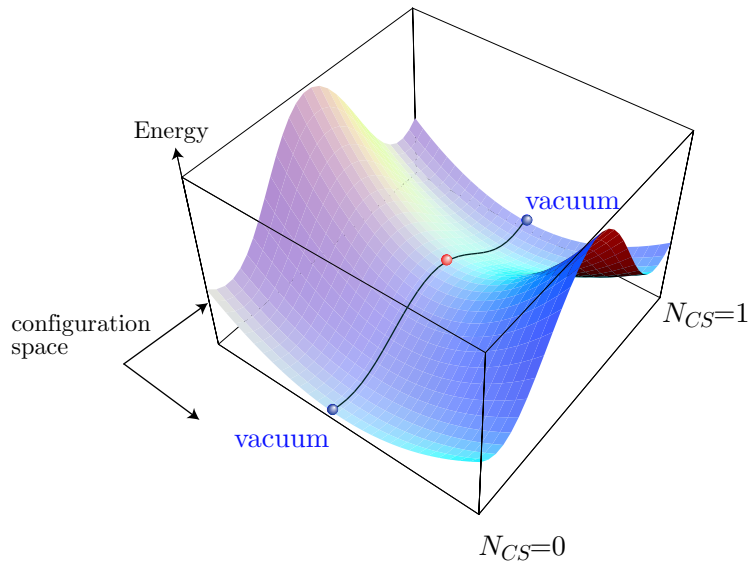
- $T < T_C$: EW phase transition temperature (broken phase)

$$\Gamma_{\text{sph}}^{(b)} \simeq T e^{-E_{\text{sph}}/T}$$

- $T > T_C$ (symmetric phase)

$$\Gamma_{\text{sph}}^{(s)} \simeq \kappa \alpha_W^4 T \quad \text{with } \kappa \sim O(1)$$

sphaleron = static **saddle-point** solution of $SU(2)$ -gauge-Higgs system

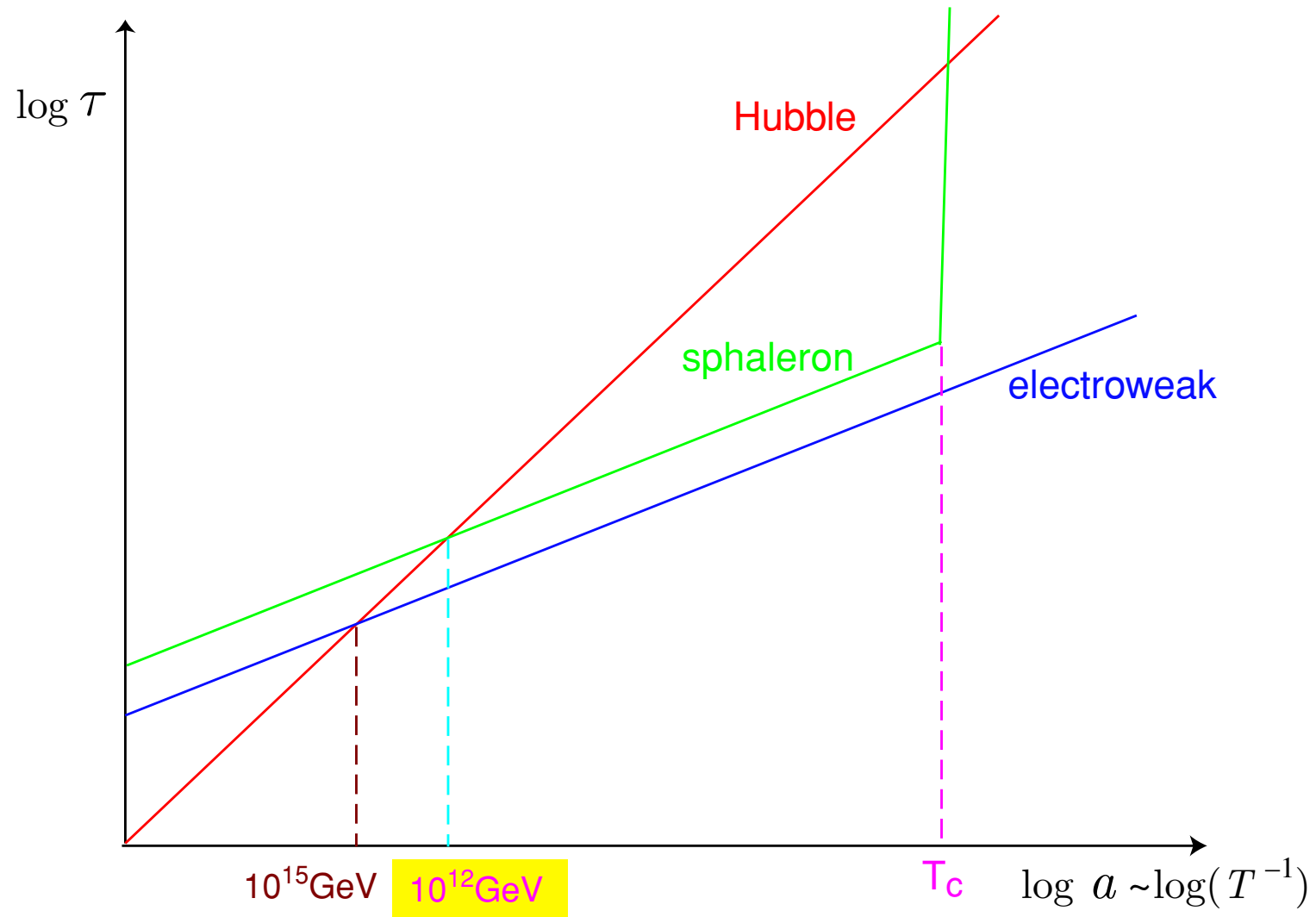


$$E_{\text{sph}} = O(1)\text{TeV}$$

first found by Manton [[Phys. Rev. D28 \('83\)](#)]

Now found in the MSSM (2HDM),
the Next-to-MSSM

time scale of the sphaleron transition vs that of the expansion



For $T_C < T < 10^{12}\text{GeV}$, $\Gamma_{\text{sph}}^{(s)} > H(T)$

$\implies B \propto (B - L)_{\text{primordial}}$ at $T \leq T_C$

\therefore For the matter in the Universe to be left at present, either

- (i) $B - L \neq 0$ must exist **before the sphaleron process decouples**, or
- (ii) $B + L$ must be generated at the EW phase transition **and the sphaleron process becomes ineffective after that.**

(i) $\implies (B - L)$ -violating GUTs, Leptogenesis

(ii) \implies Electroweak baryogenesis

sphaleron decoupling condition: $\Gamma_{\text{sph}}^{(b)}(T_C) < H(T_C)$

\longrightarrow lower bound on $E_{\text{sph}}(T_C) \propto v(T_C)$ ($v(T) = \langle \Phi \rangle$; $\Phi =$ Higgs doublet)

\longrightarrow upper bound on the Higgs mass (see below)

§4. Electroweak baryogenesis

— closely related to the particle physics at the weak scale

- (i) Baryon number violation \longleftarrow sphaleron process **in the symmetric phase**
must decouple just after the EW phase transition
- (ii) C and CP violation \longleftarrow KM phase, or complex parameters in extended models
- (iii) Out of equilibrium \longleftarrow sphaleron process can be out of equilibrium at the EWPT
if $E_{\text{sph}}(T_C)/T_C$ is sufficiently large
— **strongly first-order PT**

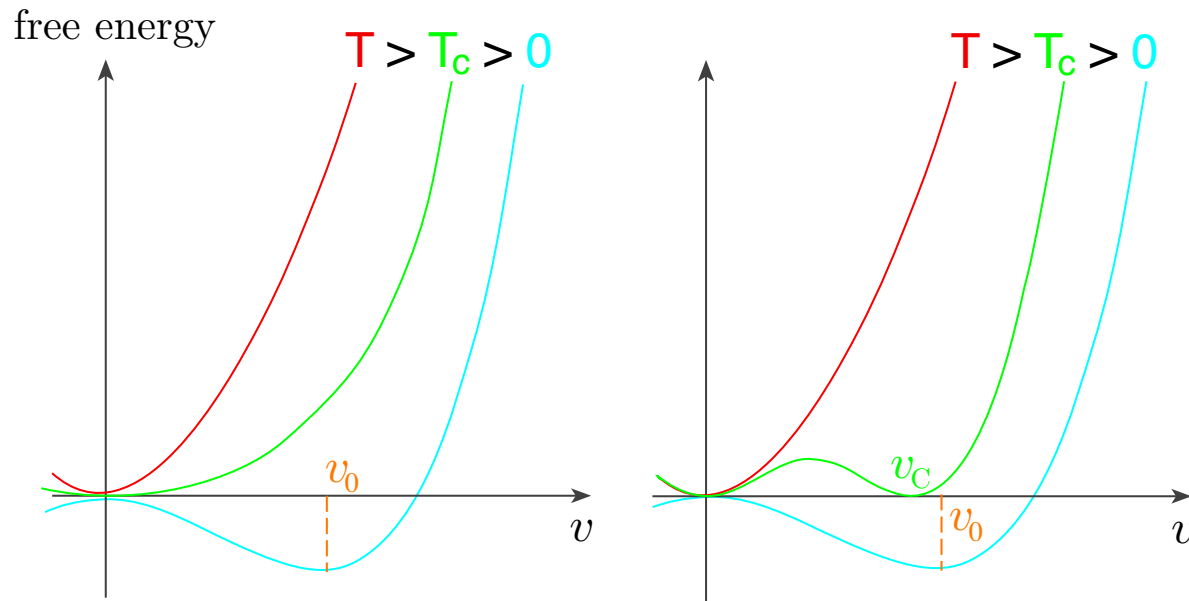
As we shall see, the conditions (ii) and (iii) require an extension of the standard model, because

- ★ KM phase is insufficient to produce the present BAU
- ★ EWPT is not of first order for the Higgs mass $m_h > 114\text{GeV}$ (LEP bound)

for reviews , see

- KF, Prog. Theor. Phys. 96 (1996) 475
- Riotto and Trodden, Ann. Rev. Nucl. Part. Sci. 49 (1999) [hep-ph/9901362]
- Bernreuther, Lec. Notes Phys. 591 (2002) 237 [hep-ph/0205279]

Electroweak phase transition (EWPT)



Standard Model

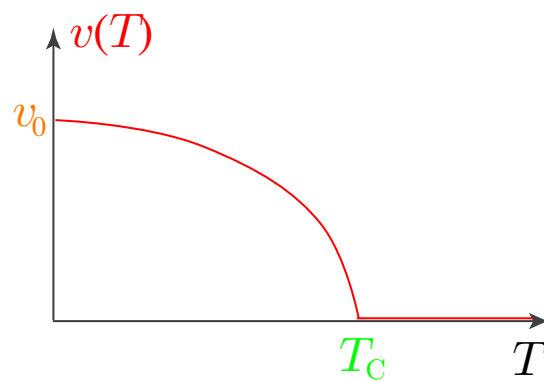
order parameter:

$$\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \varphi \end{pmatrix}$$

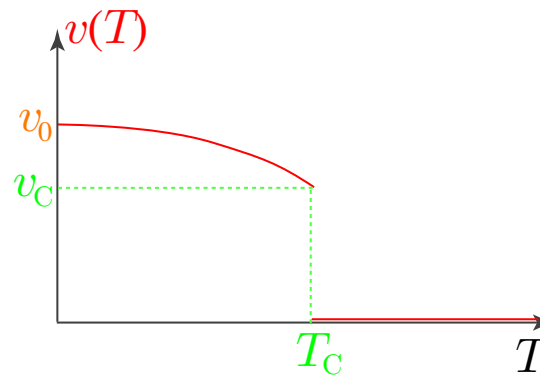
\therefore 1st order EWPT



$$v_c \equiv \lim_{T \uparrow T_c} \varphi(T) \neq 0$$



2nd order PT



1st order PT

Minimal SM — perturbation at the 1-loop level (W , Z , top quark loop)

$$V_{\text{eff}}(\varphi; T) = -\frac{1}{2}\mu^2\varphi^2 + \frac{\lambda}{4}\varphi^4 + 2Bv_0^2\varphi^2 + B\varphi^4 \left[\log\left(\frac{\varphi^2}{v_0^2}\right) - \frac{3}{2} \right] + \bar{V}(\varphi; T)$$

where $B = \frac{3}{64\pi^2 v_0^4} (2m_W^4 + m_Z^4 - 4m_t^4),$

$$\bar{V}(\varphi; T) = \frac{T^4}{2\pi^2} [6I_B(a_W) + 3I_B(a_Z) - 6I_F(a_t)], \quad (a_A = m_A(\varphi)/T)$$

$$I_{B,F}(a) \equiv \int_0^\infty dx x^2 \log\left(1 \mp e^{-\sqrt{x^2+a^2}}\right).$$

high-temperature expansion [$m/T \ll 1$]

$$\gamma_E = 0.5772 \dots$$

$$I_B(a) = -\frac{\pi^4}{45} + \frac{\pi^2}{12}a^2 - \frac{\pi}{6}(a^2)^{3/2} - \frac{a^4}{16} \log \frac{\sqrt{a^2}}{4\pi} - \frac{a^4}{16} \left(\gamma_E - \frac{3}{4} \right) + O(a^6)$$

$$I_F(a) = \frac{7\pi^4}{360} - \frac{\pi^2}{24}a^2 - \frac{a^4}{16} \log \frac{\sqrt{a^2}}{\pi} - \frac{a^4}{16} \left(\gamma_E - \frac{3}{4} \right) + O(a^6)$$

Applying the high-T expansion assuming $T > m_W, m_Z, m_t$,

$$V_{\text{eff}}(\varphi; T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4$$

where

$$D = \frac{1}{8v_0^2}(2m_W^2 + m_Z^2 + 2m_t^2), \quad E = \frac{1}{4\pi v_0^3}(2m_W^3 + m_Z^3) \sim 10^{-2}$$

$$\lambda_T = \lambda - \frac{3}{16\pi^2 v_0^4} \left(2m_W^4 \log \frac{m_W^2}{\alpha_B T^2} + m_Z^4 \log \frac{m_Z^2}{\alpha_B T^2} - 4m_t^4 \log \frac{m_t^2}{\alpha_F T^2} \right)$$

$$T_0^2 = \frac{1}{2D}(\mu^2 - 4Bv_0^2), \quad \log \alpha_{F(B)} = 2 \log(4)\pi - 2\gamma_E$$

At T_C , \exists degenerate minima: $\varphi_C = \frac{2ET_C}{\lambda_{T_C}}$

$$\Gamma_{\text{sph}}^{(\text{br})} < H(T_C) \iff \frac{\varphi_C}{T_C} \gtrsim 1 \implies \text{upper bound on } \lambda \quad [m_H = \sqrt{2}\lambda v_0]$$

$$\longrightarrow m_H \lesssim 46 \text{ GeV} \implies \text{Minimal SM is excluded!}$$

Nonperturbative study by Lattice Gauge Theory:

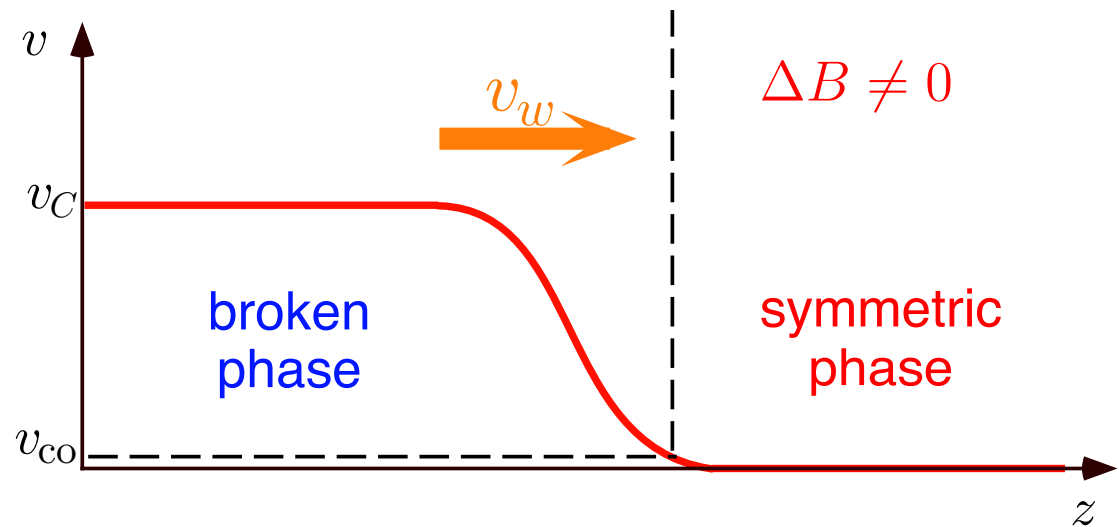
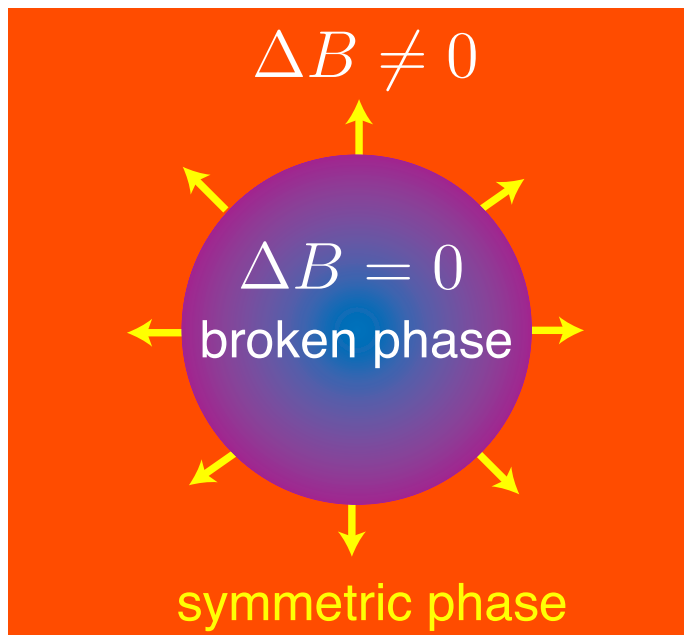
$$m_h > 73\text{GeV} \Rightarrow \text{PT disappears (crossover)}$$

∴ The EWBG does not work in the Standard Model with $m_h \geq 114\text{GeV}$.

If the EWPT is of first order,

it proceeds accompanying nucleation and growth of the bubble walls:

→ sphaleron process becomes out of equilibrium



broken phase

$$T_{R \rightarrow L}^s \rightarrow T_{R \rightarrow R}^s$$

symmetric phase

$$\psi_R$$

$$R_{R \rightarrow L}^s$$

Difference in the reflection rate for ψ_L and ψ_R

chiral charge flux into the sym. phase

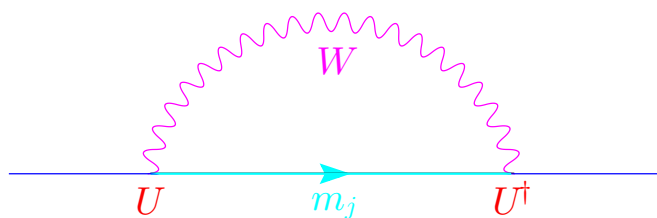
$Q_L \neq Q_R$, conserved in sym. phase: Y, I_3

bias on the sphaleron process

$B + L \neq 0$ in the symmetric phase

$B + L$ frozen in the broken phase

★ Minimal SM — CKM phase



$m_i \neq m_j$:

$O(\alpha_W)$ effect in the dispersion

[Farrar, Shaposhnikov, Phys. Rev. 50 ('94)]

▷ decoherence by QCD correction

[Gavela, et al., Nucl. Phys. B430 ('94)]

$$\left| \frac{n_B}{s} \right| < 10^{-26}$$

effective CP violation at the tree level

- ★ relative phase of Higgs doublets in the extended models

$$m_f(x) = y_f |\phi(x)| e^{i\theta(x)} \text{ — spacetime-dependent phase}$$

- ★ complex parameters in the mass matrices of SUSY particles

$$e.g. \text{ chargino: } M_{\chi^\pm} = \begin{pmatrix} M_2 & -\frac{i}{\sqrt{2}}g_2 v_u e^{-i\theta} \\ -\frac{i}{\sqrt{2}}g_2 v_d & -\mu \end{pmatrix}$$

x -dependent v_d and v_u \longrightarrow effectively x -dependent phases

For the EWBG to work, we need an extension of the Standard Model.

- ▷ Higgs sector — MSSM: $m_{H_1} \leq 120\text{GeV}$ and a light stop $m_{\tilde{t}_1} \leq m_t$
2HDM, NMSSM: possible for $m_h > 130\text{GeV}$
- ▷ CP violation — Higgs doublets more than 2
complex parameters in the SUSY models