

# Electroweak Baryogenesis

— recent results in the MSSM and NMSSM —

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## Baryon Asymmetry of the Universe

$$\frac{n_B}{s} \equiv \frac{n_b - n_{\bar{b}}}{s} \simeq (0.37 - 0.88) \times 10^{-10}$$

# Big Bang Nucleosynthesis

$$Y = \frac{2n}{n+p} \quad (= 0.25 \leftrightarrow \frac{n}{p} = \frac{1}{7})$$

- $T \gg 1\text{MeV}: n + \nu_e \leftrightarrow p + e \Rightarrow \frac{n}{p} = 1$

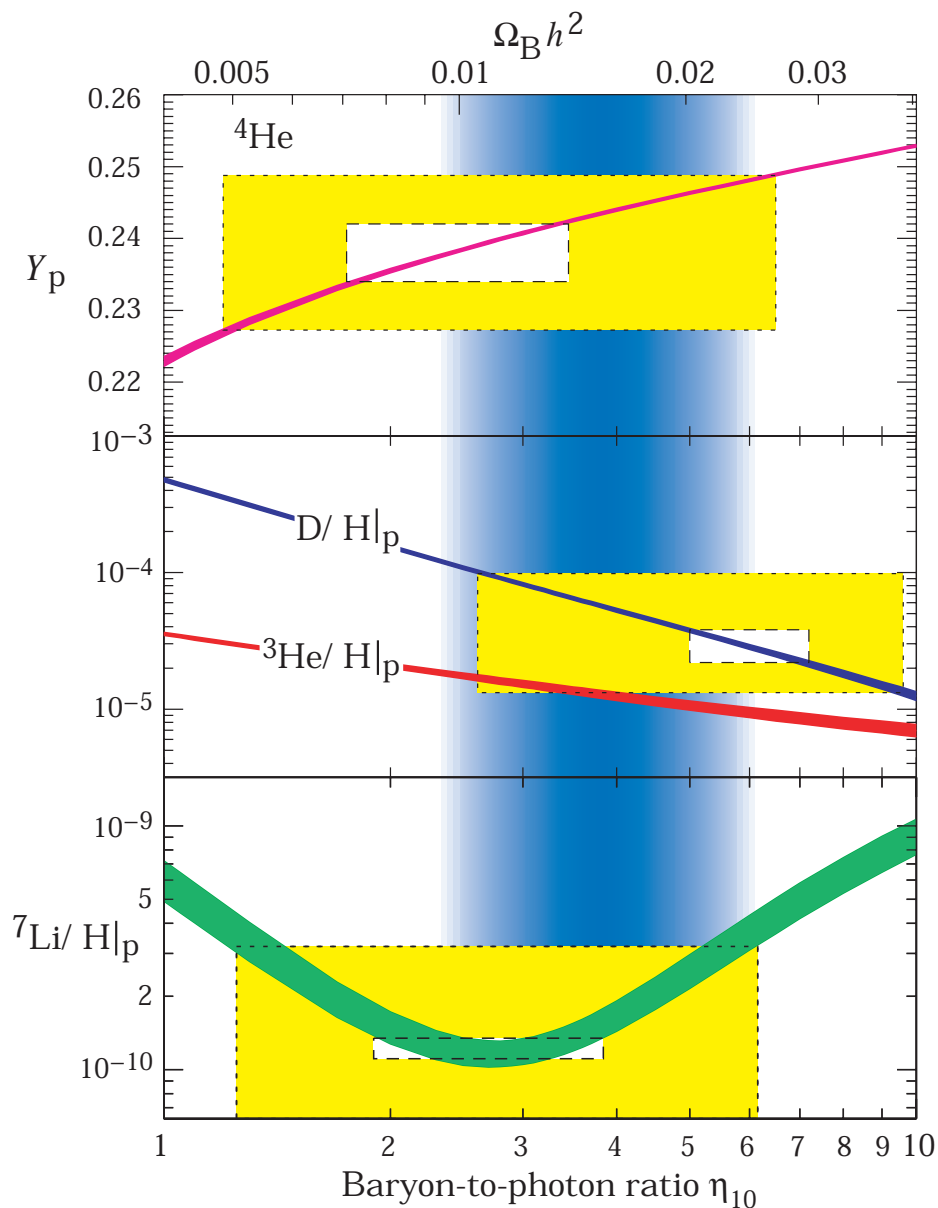
- $T = T_F \simeq 1\text{MeV}: \Gamma_{n \leftrightarrow p}(T_F) \simeq H$

$$\left. \frac{n}{p} \right|_{\text{freeze-out}} = e^{-(m_n - m_p)/T_F} \simeq \frac{1}{6}$$

- $T = 0.3 - 0.1\text{MeV}$

$$\frac{n}{p} \rightarrow \frac{1}{6} - \frac{1}{7} \quad \text{dependeing on } \eta = \frac{n_B}{n_\gamma}$$

cf.  $s \simeq 7n_\gamma$  today



## evidence of **BAU**

[Steigman, Ann.Rev.Astron.Astrop.**14**('76)]

1. no anti-matter in cosmic rays from our galaxy  
some anti-matter consistent as secondary products
2. nearby clusters of galaxies are stable  
a cluster:  $(1 \sim 100) M_{\text{galaxy}} \simeq 10^{12 \sim 14} M_{\odot}$

Starting from a  $B$ -symmetric universe ...

$$\begin{aligned} \frac{n_b}{s} \simeq \frac{n_{\bar{b}}}{s} &\sim 8 \times 10^{-11} \quad \text{at } T = 38\text{MeV} \\ &\sim 7 \times 10^{-20} \quad \text{at } T = 20\text{MeV} \quad N\bar{N}\text{-annihilation decouple} \end{aligned}$$

At  $T = 38\text{MeV}$ , mass within a causal region =  $10^{-7} M_{\odot} \ll 10^{12} M_{\odot}$ .

We must have the BAU  $\frac{n_B}{s} = (0.37 - 0.88) \times 10^{-10}$   
before the universe was cooled down to  $T \simeq 38\text{MeV}$

- **Introduction**
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# Introduction

★ Review of the Big Bang Cosmology

**Friedmann Universe** — uniform and isotropic space

$$ds^2 = dt^2 - a^2(t) \left[ \frac{dr^2}{1 - kr^2} + r^2(d\theta^2 + \sin^2 \theta d\phi^2) \right]$$

$a(t)$  : scale factor in the comoving coordinate

$k = 1, 0, -1$  : closed, flat, open space

$$\text{Einstein eq.} \Rightarrow \begin{cases} H^2 = \left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi G}{3} \rho - \frac{k}{a^2} + \frac{\Lambda}{3}, \\ \frac{\ddot{a}}{a} = -\frac{4\pi G}{3} (\rho + 3p) + \frac{\Lambda}{3} \end{cases}$$

$$\text{energy cons.} \Rightarrow a^3 \frac{dp}{dt} = \frac{d}{dt} [a^3 (\rho + p)] \Rightarrow \frac{d}{dt} (\rho a^{3(1+\gamma)}) = 0$$

$\rho$  = energy density,  $p$  = isotropic pressure

$$p = \gamma\rho \quad \text{with} \quad \begin{cases} \gamma = 1/3 & \text{(RD universe)} \\ \gamma \ll 1 & \text{(MD universe)} \end{cases}$$

For RD universe,

$$\int \frac{d^3\mathbf{k}}{(2\pi)^3} \frac{|\mathbf{k}|}{e^{|\mathbf{k}|/T} \mp 1} = \begin{cases} \frac{\pi^2}{30} T^4, \\ \frac{7}{8} \frac{\pi^2}{30} T^4, \end{cases} \Rightarrow \rho(T) = \frac{\pi^2}{30} g_* T^4 \quad \text{with} \quad g_* \equiv \sum_B g_B + \frac{7}{8} \sum_F g_F$$

For the EW theory with  $N_f$  generations and  $m$  Higgs doublets,

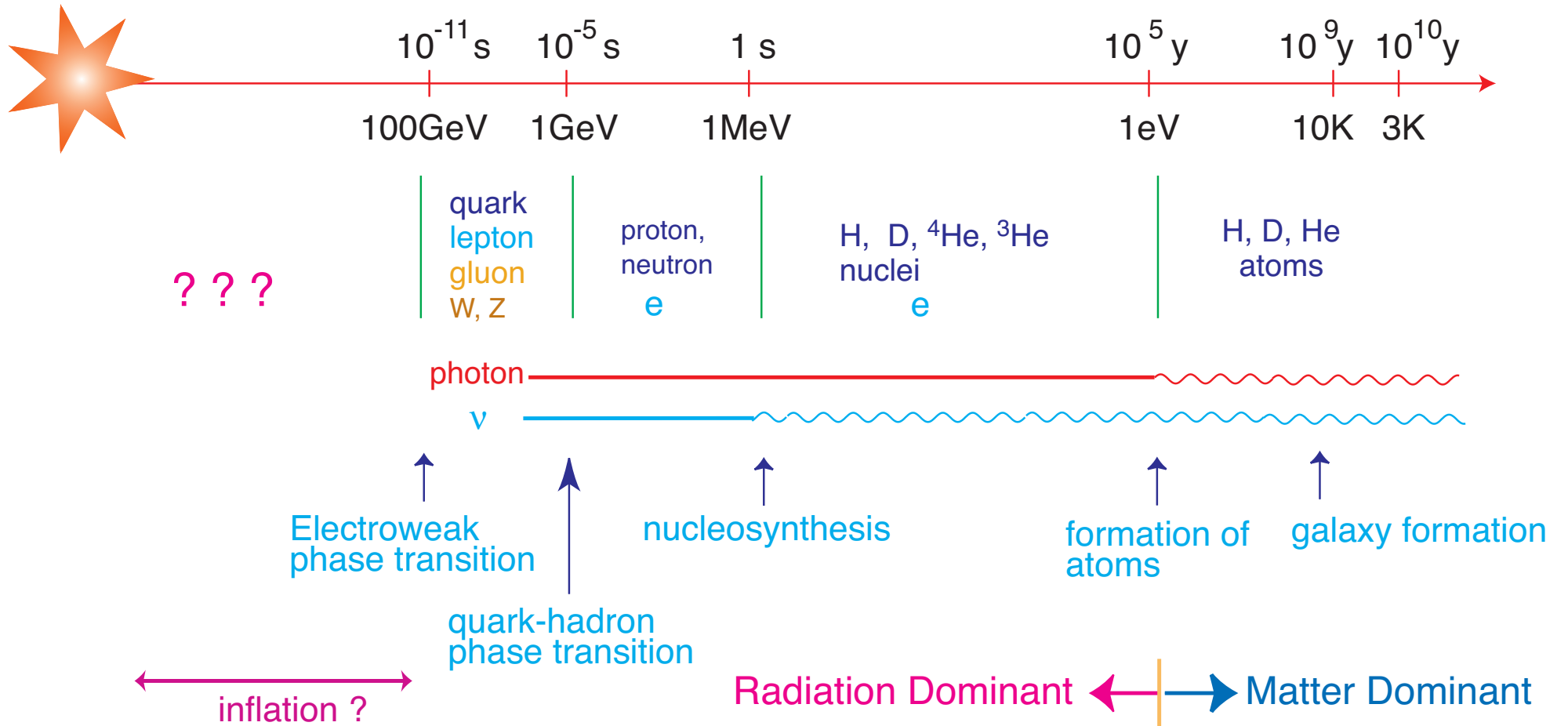
$$g_* = 24 + 4m + \frac{7}{8} \times 30N_f$$

so that  $g_* = 106.75$  for the Minimal SM.

In RD universe, neglecting  $\Lambda$ ,

$$H \simeq \sqrt{\frac{8\pi G}{3} \rho} \simeq 1.66 \sqrt{g_*} \frac{T^2}{m_{Pl}}$$

$$m_{Pl} = G^{-1/2} = 1.22 \times 10^{19} \text{ GeV}$$



- (1) baryon number violation
- (2)  $C$  and  $CP$  violation
- (3) departure from equilibrium

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$\therefore$  (2) If  $C$  or  $CP$  is conserved, no  $B$  is generated:  $\Leftarrow B$  is odd under  $C$  and  $CP$ .

indeed ...

$\rho_0$  : baryon-symmetric initial state of the universe *s.t.*

$$\langle n_B \rangle_0 = \text{Tr}[\rho_0 n_B] = 0$$

time evolution of  $\rho \iff$  Liouville eq.:  $i\hbar \frac{\partial \rho}{\partial t} + [\rho, H] = 0$

If  $H$  is  $C$ - or  $CP$ -invariant,  $[\rho, C] = 0$  or  $[\rho, CP] = 0$  [spont.  $CP$  viol.  $\Rightarrow [\rho, CP] \neq 0$ ]



Since  $CB C^{-1} = -B$  and  $CP B (CP)^{-1} = -B$  [i.e.,  $B$  is vectorlike, odd under  $C$ .]

$$\langle n_B \rangle = \text{Tr}[\rho n_B] = \text{Tr}[\rho C n_B C^{-1}] = -\text{Tr}[\rho n_B]$$

*or*

$$\langle n_B \rangle = \text{Tr}[\rho CP n_B (CP)^{-1}] = -\text{Tr}[\rho n_B]$$

$\therefore$  Both  $C$  and  $CP$  must be violated to have  $\langle n_B \rangle \neq 0$ , starting from  $\langle n_B \rangle_0 = 0$ .

## possibilities ?

- $B$  violation  $\left\{ \begin{array}{ll} \text{explicit violation} & \text{GUTs} \\ \text{spontaneous viol.} & \langle \text{squark} \rangle \neq 0 \\ \text{chiral anomaly} & \text{sphaleron process} \end{array} \right.$

It must be **suppressed at present** for **protons not to decay**.

- $C$  violation  $\Leftarrow$  chiral gauge interactions (EW, GUTs)

- $CP$  violation  $\left\{ \begin{array}{l} \text{KM phase in the MSM} \\ \text{beyond the SM — SUSY, extended Higgs sector} \end{array} \right.$

- out of equilibrium  $\left\{ \begin{array}{l} \text{expansion of the universe} \\ \text{first-order phase transition} \\ \text{reheating (or preheating) after inflation} \end{array} \right. \quad \Gamma_{\Delta B \neq 0} \simeq H(T)$

$SU(5)$  model:

$$\text{matter: } \begin{cases} \mathbf{5}^* : \psi_L^i & \ni d_R^c, l_L \\ \mathbf{10} : \chi_{[ij]L} & \ni q_L, u_R^c, e_R^c \\ i = 1 - 5 & \rightarrow (\alpha = 1 - 3, a = 1, 2) \end{cases} \quad \text{gauge: } A_\mu = \begin{pmatrix} G_\mu, B_\mu & X_\mu^{a\alpha} \\ X_\mu^{a\alpha} & W_\mu, B_\mu \end{pmatrix}$$

$$\begin{aligned} \mathcal{L}_{\text{int}} &\ni g \bar{\psi} \gamma^\mu A_\mu \psi + g \text{Tr} [\bar{\chi} \gamma^\mu \{A_\mu, \chi\}] \\ &\ni g X_{\alpha\mu}^a [\varepsilon^{\alpha\beta\gamma} \bar{u}_{R\gamma}^c \gamma^\mu q_{L\beta a} + \epsilon_{ab} (\bar{q}_{Lb}^\alpha \gamma^\mu e_R^c + \bar{l}_{Lb} \gamma^\mu d_R^{c\alpha})] \end{aligned}$$

in the decay of  $X$ - $\bar{X}$  pairs

$$\langle \Delta B \rangle = \frac{2}{3}r - \frac{1}{3}(1-r) - \frac{2}{3}\bar{r} + \frac{1}{3}(1-\bar{r}) = r - \bar{r}$$

$\therefore C$  or  $CP$  is conserved ( $r = \bar{r}$ )  
 $\implies \Delta B = 0$

process	br. ratio	$\Delta B$
$X \longrightarrow qq$	$r$	$2/3$
$X \longrightarrow \bar{q}\bar{l}$	$1-r$	$-1/3$
$\bar{X} \longrightarrow \bar{q}\bar{q}$	$\bar{r}$	$-2/3$
$\bar{X} \longrightarrow q, l$	$1-\bar{r}$	$1/3$

If the inverse process is suppressed,  $B \propto r - \bar{r}$  is generated.

At  $T \simeq m_X$ , decay rate of  $X$   $= \Gamma_D \simeq \alpha m_X$       $\alpha \sim 1/40$  for gauge boson,

$\Gamma_D \simeq H(T \simeq m_X) \implies$  decay and production of  $X\bar{X}$  are **out of equilibrium**

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The  $SU(5)$  GUT model **conserves  $B - L$** .     *i.e.*  $(B + L)$ -genesis



Any  $B$  is washed-out by the sphaleron process, as we shall see later



new varieties of baryogenesis

*e.g.* Leptogenesis  $\implies$  **BAU**      $B = -L$

- $\exists$  Majorana neutrino  $\Rightarrow L$ -violating interaction [Fukugita & Yanagida, PL174B]
 

$\left. \begin{array}{l} \text{decoupling of heavy-}\nu \text{ decay} \\ CP \text{ violation in the heavy } -\nu \text{ sector} \end{array} \right\} \Rightarrow$	$\text{Leptogenesis} \xRightarrow{\text{sphaleron}} \text{BAU}$
	[review: Buchmüller et al., hep-ph/0401240]
- Affleck-Dine mechanism in a SUSY model [A-D, NPB249; Dine, et al., NPB458]
 

$\langle \tilde{q} \rangle \neq 0$  or  $\langle \tilde{l} \rangle \neq 0$  along (nearly) flat directions, at high temperature  
 coherent motion of complex  $\langle \tilde{q} \rangle, \langle \tilde{l} \rangle \neq 0$   $B(L), C, CP$  viol.  
 $\Rightarrow B$ - and/or  $L$ -genesis
- Electroweak Baryogenesis
  - (1)  $\Delta(B + L) \neq 0$ 

{	enhanced by sphaleron at $T > T_C$ suppressed by instanton at $T = 0$
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  - (2)  $C$ -violation (chiral gauge);  $CP$ -violation: KM phase or extension of the MSM
  - (3) first-order EWPT with expanding bubble walls
- topological defects  
 EW string, domain wall  $\sim$  EW baryogenesis effective volume is too small

# Sphaleron Process

★ Anomalous fermion number nonconservation

← axial anomaly in the SM

$$\partial_\mu j_{B+L}^\mu = \frac{N_f}{16\pi^2} [g^2 \text{Tr}(F_{\mu\nu} \tilde{F}^{\mu\nu}) - g'^2 B_{\mu\nu} \tilde{B}^{\mu\nu}]$$

$$\partial_\mu j_{B-L}^\mu = 0$$

$N_f$  = number of the generations  
 $\tilde{F}^{\mu\nu} \equiv \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$

integrating these equations,

$$B(t_f) - B(t_i) = \frac{N_f}{32\pi^2} \int_{t_i}^{t_f} d^4x \left[ g^2 \text{Tr}(F_{\mu\nu} \tilde{F}^{\mu\nu}) - g'^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \right]$$

$$= N_f [N_{CS}(t_f) - N_{CS}(t_i)]$$

where  $N_{CS}$  is the Chern-Simons number:  
in the  $A_0 = 0$  gauge,

$$N_{CS}(t) = \frac{1}{32\pi^2} \int d^3x \epsilon_{ijk} \left[ g^2 \text{Tr} \left( F_{ij} A_k - \frac{2}{3} g A_i A_j A_k \right) - g'^2 B_{ij} B_k \right]_t$$

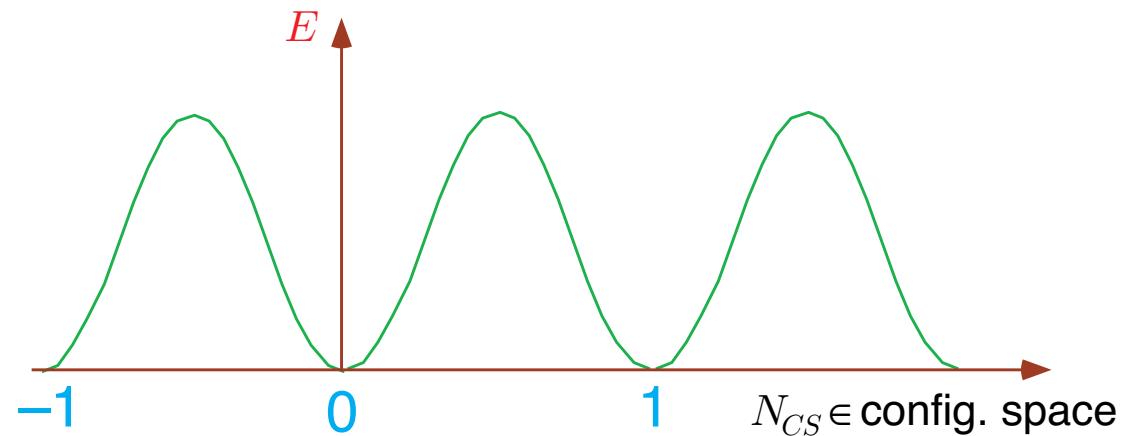
classical vacua of the gauge sector:  $\mathcal{E} = \frac{1}{2}(\mathbf{E}^2 + \mathbf{B}^2) = 0 \iff F_{\mu\nu} = B_{\mu\nu} = 0$

$\iff A = iU^{-1}dU$  and  $B = dv$  with  $U \in SU(2)$

$\therefore U(\mathbf{x}) : S^3 \ni \mathbf{x} \longrightarrow U \in SU(2) \simeq S^3$

$\pi_3(S^3) \simeq \mathbf{Z} \implies U(\mathbf{x})$  is classified by an integer  $N_{CS}$ .

energy functional vs configuration space

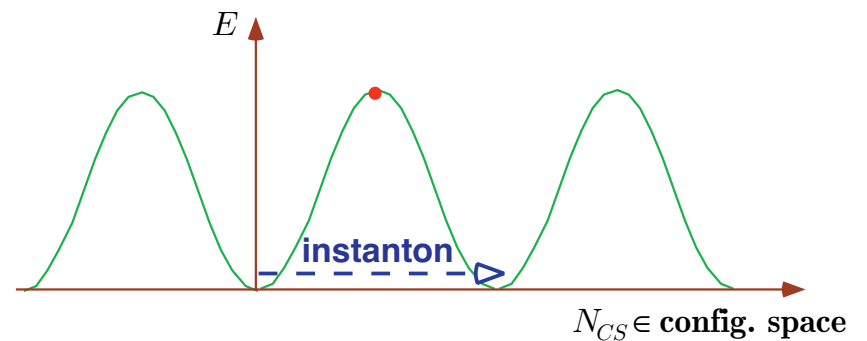


background  $U$  changes with  $\Delta N_{CS} = 1$   
 $\implies \Delta B = 1$  ( $\Delta L = 1$ ) in each (left-) generation

$\iff$  fermion:  
 {  
 • level crossing  
 • index theorem

Transition of the field config. with  $\Delta B \neq 0$

- ▷ quantum tunneling      low temperature
- ▷ thermal activation      high temperature



transition rate with  $N_{CS} = 1 \iff$  WKB approx.

At  $T = 0$ ,

$$\text{tunneling amplitude} \simeq e^{-S_{\text{instanton}}} = e^{-4\pi^2/g^2}$$

instanton

- ★ stable
- ★ 4d solution with finite euclidean action
- ★ integer Pontrjagin index  $\sim \int d^4x_E F_{\mu\nu} \tilde{F}^{\mu\nu}$



## What is Sphaleron ?

sphaleros :  $\sigma\varphi\alpha\lambda\epsilon\rho\sigma$  = 'ready to fall'

a saddle-point solution of 4d  $SU(2)$  gauge-Higgs system

[Klinkhammer & Manton, PRD30 ('84)]

$$E_{\text{sph}} = 8 - 14 \text{ TeV}$$

- ★ unstable
- ★ static (3d) solution with finite energy
- ★ Chern-Simons No. = "1/2"

⇒ over-barrier transition at finite temperature

$$\Gamma_{\text{sph}} \sim e^{-E_{\text{sph}}/T}$$

cf. for EW theory

$$\Gamma_{\text{tunneling}} \sim e^{-2S_{\text{instanton}}} = 10^{-164}$$

★ Transition rate

[Arnold and McLerran, P.R.D36('87)]

$$\clubsuit \frac{\omega_-}{(2\pi)} \lesssim T \lesssim T_C$$

$\omega_-$ : negative-mode freq. around the sphaleron

$$\Gamma_{\text{sph}}^{(b)} \simeq k \mathcal{N}_{\text{tr}} \mathcal{N}_{\text{rot}} \frac{\omega_-}{2\pi} \left( \frac{v^2}{T} \right)^3 e^{-E_{\text{sph}}/T}$$

$$\mathcal{N}_{\text{tr}} = 26, \mathcal{N}_{\text{rot}} = 5.3 \times 10^3 \leftarrow \text{zero modes}$$

$$\omega_-^2 \simeq (1.8 \sim 6.6) m_W^2 \text{ for } 10^{-2} \leq \lambda/g^2 \leq 10, \quad k \simeq O(1)$$

$\clubsuit T \gtrsim T_C$  symmetric phase — no mass scale

$$\Gamma_{\text{sph}}^{(s)} \simeq \kappa (\alpha_W T)^4$$

▷ Monte Carlo simulation

$$\langle N_{CS}(t) N_{CS}(0) \rangle = \langle N_{CS} \rangle^2 + A e^{-2\Gamma V t} \text{ as } t \rightarrow \infty$$

$\kappa > 0.4$   $SU(2)$  gauge-Higgs system [Ambjørn, et al. N.P.B353('91)]

$\kappa = 1.09 \pm 0.04$   $SU(2)$  pure gauge system [Ambjørn and Krasnitz, P.L.B362('95)]

**'sphaleron transition'** even in the symmetric phase.

## B and L in the Hot Universe

reaction rate:  $\Gamma(T) > H(t) \iff$  the process is in **chemical equilibrium**

$$H(t) \equiv \frac{\dot{a}(t)}{a(t)} \simeq \sqrt{\frac{8\pi G}{3} \rho} \simeq 1.66 \sqrt{g_*} \frac{T^2}{m_{Pl}}$$

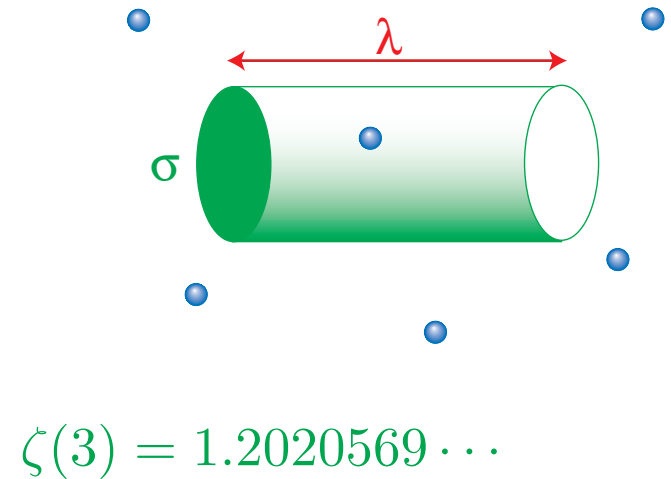
$\Gamma(T) \rightarrow$  time scale of interactions

mean free path :  $\lambda \cdot \sigma = \frac{1}{n}$

$m \ll T \Rightarrow \lambda \simeq \bar{t} =$  mean free time

$$n = g \int \frac{d^3 \mathbf{k}}{(2\pi)^3} \frac{1}{e^{\omega_k/T} \mp 1} \quad \begin{matrix} m \ll T \\ \simeq \\ g \end{matrix} \begin{cases} \frac{\zeta(3)}{\pi^2} T^3 \\ \frac{3}{4} \frac{\zeta(3)}{\pi^2} T^3 \end{cases}$$

$$\begin{matrix} m \gg T \\ \simeq \\ g \end{matrix} \left( \frac{mT}{2\pi} \right)^{3/2} e^{-m/T}$$



For relativistic particles at  $T$ ,  $\sigma \simeq \frac{\alpha^2}{s} \simeq \frac{\alpha^2}{T^2}$ , we have  $\lambda \simeq \frac{10}{gT^3} \left( \frac{\alpha^2}{T^2} \right)^{-1} = \frac{10}{g\alpha^2 T}$ .

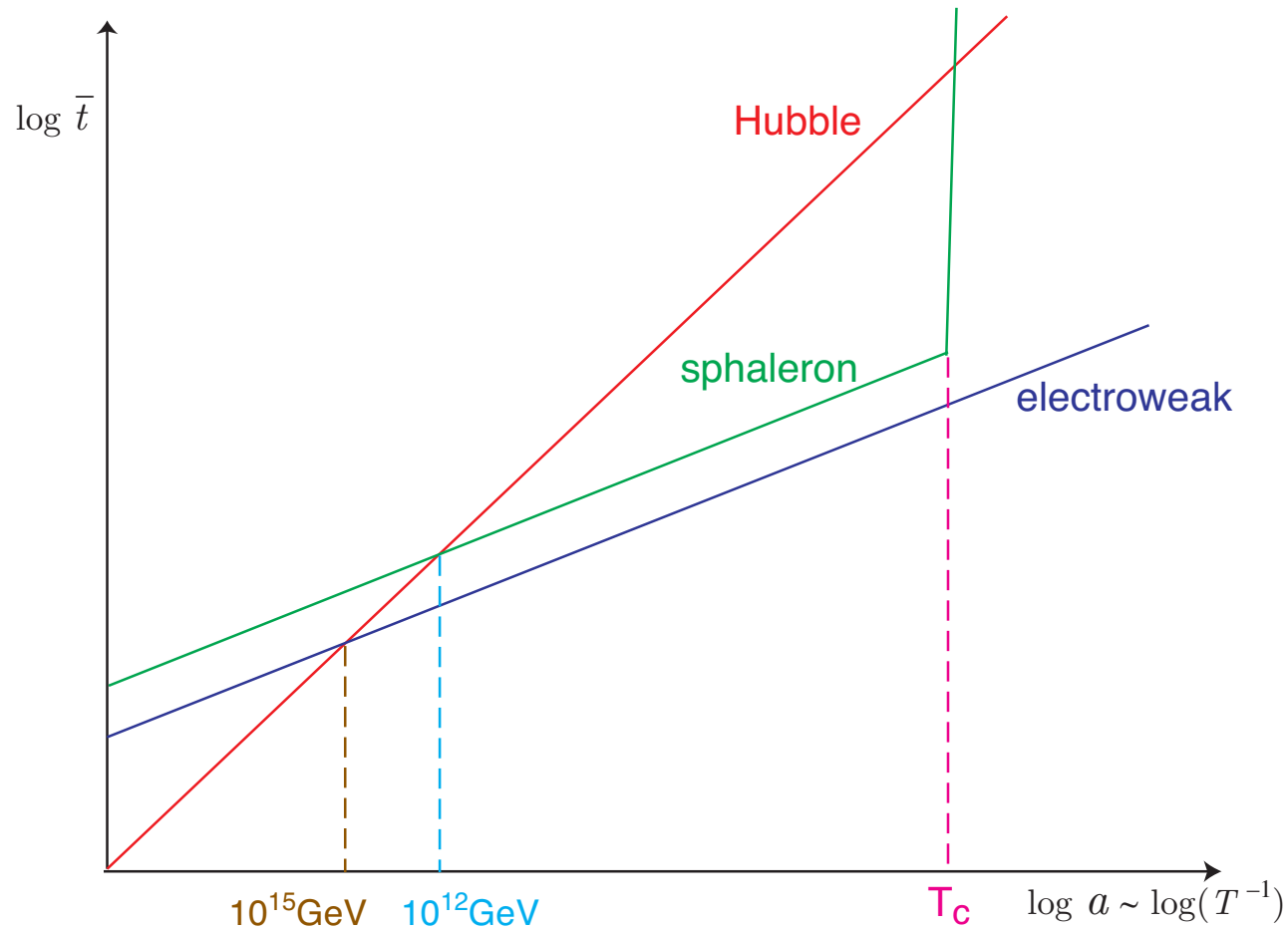
For  $T = 100\text{GeV}$ ,  $H^{-1} \simeq 10^{14}\text{GeV}^{-1}$ ,

$\lambda_s \simeq \frac{1}{\alpha_s^2 T} \sim 1 \text{ GeV}^{-1}$	for strong interactions
$\lambda_{EW} \simeq \frac{1}{\alpha_W^2 T} \sim 10 \text{ GeV}^{-1}$	for EW interactions
$\lambda_Y \simeq \left( \frac{m_W}{m_f} \right)^4 \lambda_{EW}$	for Yukawa interactions

time scale of sphaleron process

$$\bar{t}_{\text{sph}} = (\Gamma_{\text{sph}}/n)^{-1} \simeq \begin{cases} 10^6 T^{-1} \text{ GeV}^{-1} & (T > T_C) \\ 10^5 T^{-1} e^{E_{\text{sph}}/T} \text{ GeV}^{-1} & (T < T_C) \end{cases}$$

[cf.  $E_{\text{sph}} \simeq 10\text{TeV}$  for  $v_0 = 246\text{GeV}$ ]



If  $v(T_C) \ll 200 \text{ GeV}$  (eg. 2nd order EWPT),  $\exists T_{\text{dec}}, s.t.$

$$T_{\text{dec}} < T < T_C \implies \Gamma_{\text{sph}}^{(b)}(T) > H(T)$$

wash-out of  $B + L$  even in the broken phase

## ★ Quantum numbers in equilibrium

$Q_i$ : conserved quantum number  $[H, Q_i] = 0$

equilibrium partition function:  $Z(T, \mu) \equiv \text{Tr} \left[ e^{-(H - \sum_i \mu_i Q_i)/T} \right]$

$$\Rightarrow \langle Q_i \rangle(T, \mu) = T \frac{\partial}{\partial \mu_i} \log Z(T, \mu)$$

→ relations among  $\mu$ 's  $\iff$  relations among  $Q$ 's

In the SM,  $Q_i = \frac{1}{N} B - L_i$  without lepton-flavor mixing.

1st-principle calculation of  $Z(T, \mu)$



- perturbation
- free-field approximation

- path integral over *all* fields
- *nonperturbative*  $B + L$  violation

[Shaposhnikov, et al, PLB387 ('96); PRD61 ('00)]

chemical potentials of the particles

number density of free particles (per degree of freedom)

$$\langle N \rangle = \int \frac{d^3 \mathbf{k}}{(2\pi)^3} \left[ \frac{1}{e^{(\omega_k - \mu)/T} \mp 1} - \frac{1}{e^{(\omega_k + \mu)/T} \mp 1} \right]$$

$$\stackrel{m \ll T}{\approx} \frac{T^3}{2\pi^2} \int_0^\infty dx \left[ \frac{x^2}{e^{x - \mu/T} \mp 1} - \frac{x^2}{e^{x + \mu/T} \mp 1} \right] \stackrel{|\mu| \ll T}{\approx} \begin{cases} \frac{T^3}{3} \cdot \frac{\mu}{T}, & \text{(bosons)} \\ \frac{T^3}{6} \cdot \frac{\mu}{T}, & \text{(fermions)} \end{cases}$$

Quantum number densities in terms of  $\mu$

[Harvey & Turner, PRD42 ('90)]

SM with  $N$  generations and  $N_H$  Higgs doublets ( $\phi^0 \phi^-$ )

$W^-$	$u_{L(R)}$	$d_{L(R)}$	$e_{iL(R)}$	$\nu_{iL}$	$\phi^0$	$\phi^-$
$\mu_W$	$\mu_{u_{L(R)}}$	$\mu_{d_{L(R)}}$	$\mu_{iL(R)}$	$\mu_i$	$\mu_0$	$\mu_-$

gauge int., Yukawa int, quark mixings are in equilibrium.

$$\mu_\gamma = \mu_Z = \mu_{\text{gluon}} = 0$$



$$(3N + 7) \mu\text{'s}$$

$$\text{gauge} \Leftrightarrow \mu_W = \mu_{d_L} - \mu_{u_L} = \mu_{iL} - \mu_i = \mu_- + \mu_0$$

$$\text{Yukawa} \Leftrightarrow \mu_0 = \mu_{u_R} - \mu_{u_L} = \mu_{d_L} - \mu_{d_R} = \mu_{iL} - \mu_{iR}$$

$2(N + 2)$  relations  $\Rightarrow N + 3$  independent  $\mu$ 's:  $(\mu_W, \mu_0, \mu_{u_L}, \mu_i)$

$$\text{sphaleron process in equilibrium: } |0\rangle \leftrightarrow \prod_i (u_L d_L d_L \nu_L)_i \Leftrightarrow N(\mu_{u_L} + 2\mu_{d_L}) + \sum_i \mu_i = 0$$

Quantum number densities [in unit of  $T^2/6$ ]

$$B = N(\mu_{u_L} + \mu_{u_R} + \mu_{d_L} + \mu_{d_R}) = 4N\mu_{u_L} + 2N\mu_W,$$

$$L = \sum_i (\mu_i + \mu_{iL} + \mu_{iR}) = 3\mu + 2N\mu_W - N\mu_0$$

$$Q = \frac{2}{3}N(\mu_{u_L} + \mu_{u_R}) \cdot 3 - \frac{1}{3}N(\mu_{d_L} + \mu_{d_R}) \cdot 3 - \sum_i (\mu_{iL} + \mu_{iR}) - 2 \cdot 2\mu_W - 2N_H\mu_-$$

$$= 2N\mu_{u_L} - 2\mu - (4N + 4 + 2N_H)\mu_W + (4N + 2N_H)\mu_0$$

$$I_3 = -(2N + N_H + 4)\mu_W \quad \mu \equiv \sum_i \mu_i$$



- $T \gtrsim T_C$  (symmetric phase)

We require  $Q = I_3 = 0$ . ( $\mu_W = 0$ )

$$B = \frac{8N + 4N_H}{22N + 13N_H} (B - L), \quad L = -\frac{14N + 9N_H}{22N + 13N_H} (B - L)$$

- $T \lesssim T_C$  (broken phase)

$Q = 0$  and  $\mu_0 = 0$  ( $\because \phi^0$  condensates.)

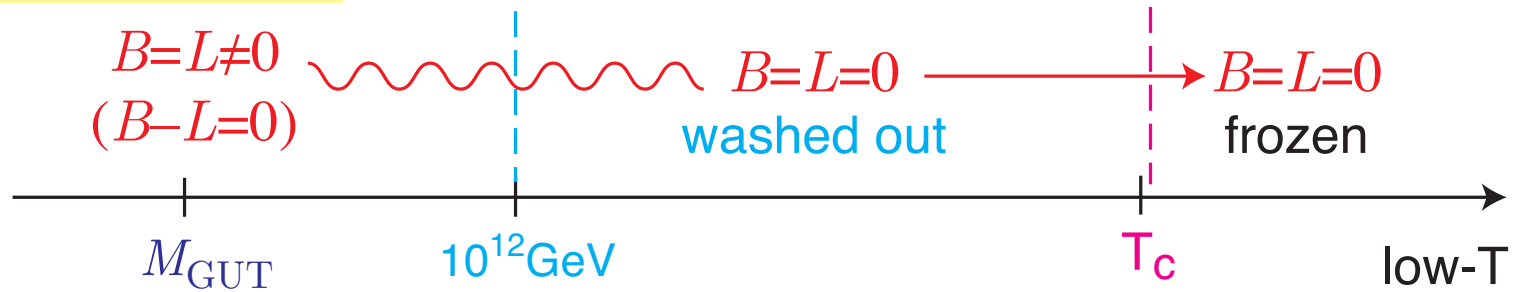
$$B = \frac{8N + 4(N_H + 2)}{24N + 13(N_H + 2)} (B - L), \quad L = -\frac{16N + 9(N_H + 2)}{24N + 13(N_H + 2)} (B - L)$$

In any case,  $B = L = 0$ , if  $(B - L)_{\text{primordial}} = 0$ .

To have nonzero BAU,

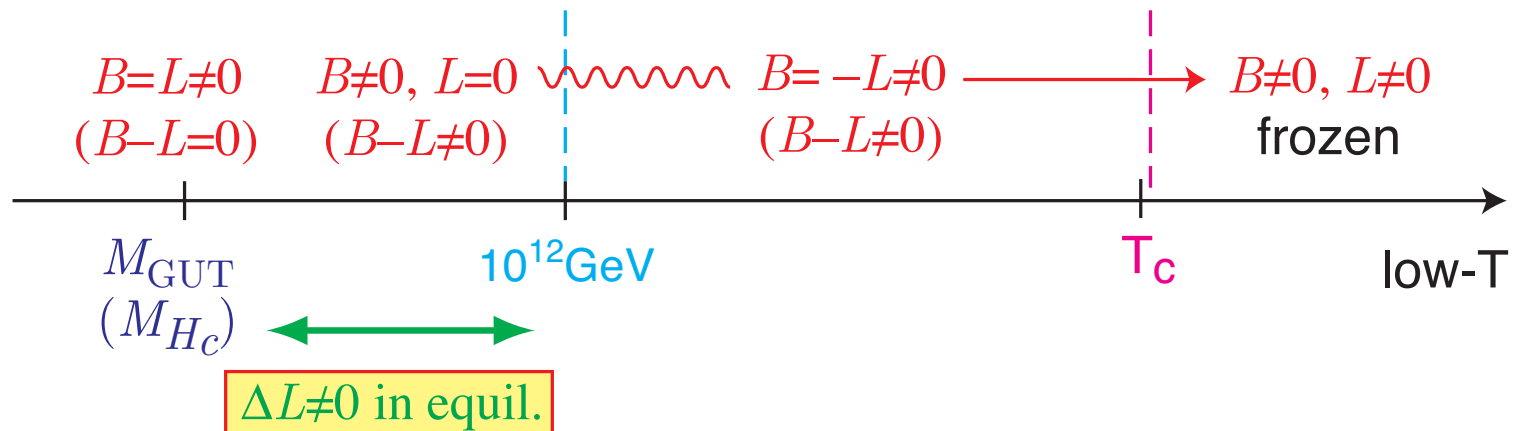
- (i) we must have  $B - L$  before the sphaleron process decouples, **or**
- (ii)  $B + L$  must be created at the first-order EWPT, **and**  
the sphaleron process must decouple immediately after that.

Wash-out of  $B$  and  $L$  in  $(B - L)$ -conserving GUTs



Resurrection of  $(B - L)$ -conserving GUT Baryogenesis

[Fukugita & Yanagida, PRL 89]



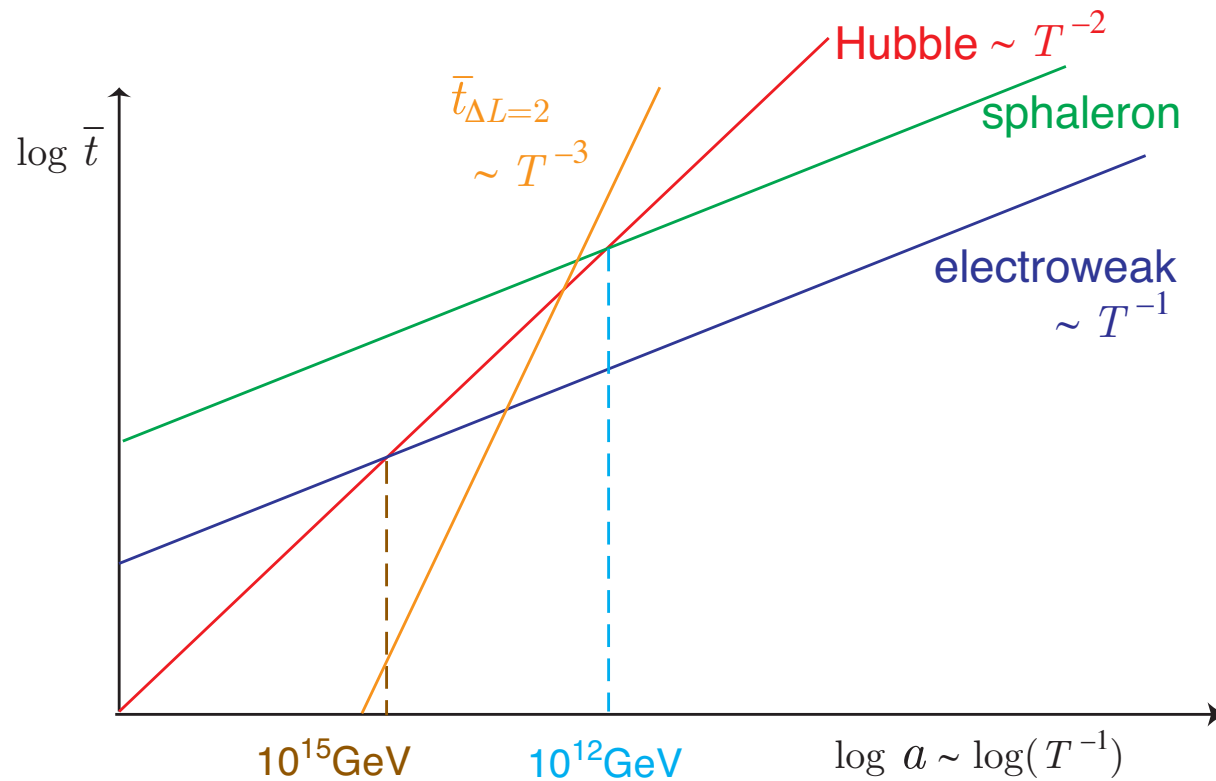
↑  
If  $\exists$  heavy Majorana  $\nu$

We must require that the processes decouple before  $T$  lowers to  $10^{12}\text{GeV}$ .  
 otherwise,  $B = L = 0!!$

e.g.,

$$\mathcal{L}_{\text{eff}} = \frac{g_i^2}{m_{N_i}} l_i \phi l_i \phi \implies \Gamma_{\Delta L=2} \simeq \frac{0.12 g_i^4 T^3}{4\pi m_{N_i}^2} < H(T) \text{ at } T < 10^{12}\text{GeV}$$

$\implies$  lower bound on  $m_{N_i} \iff m_{\nu_i} < 0.8\text{eV}$



# Electroweak Baryogenesis

## review articles:

- KF, Prog.Theor.Phys. 96 (1996) 475
- Rubakov and Shaposhnikov, Phys.Usp. 39 (1996) 461-502  
(hep-ph/9603208)
- Riotto and Trodden, Ann. Rev. Nucl. Part. Sci. 49 (1999) 35  
(hep-ph/9901362)
- Bernreuther, Lect.Notes Phys. 591 (2002) 237  
(hep-ph/0205279)

$$T \simeq 100\text{GeV} \Rightarrow H^{-1}(T) \simeq 10^{14}\text{GeV}^{-1} \ll \bar{t}_{EW} \simeq \frac{1}{\alpha_W T^2} \sim 10\text{GeV}^{-1}$$

$\therefore$  All the particles of the SM are **in equilibrium**.

nonequilibrium state  $\Leftarrow$  **1st order EW phase transition**

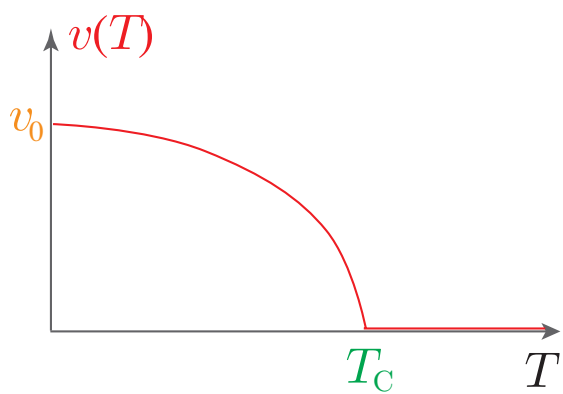
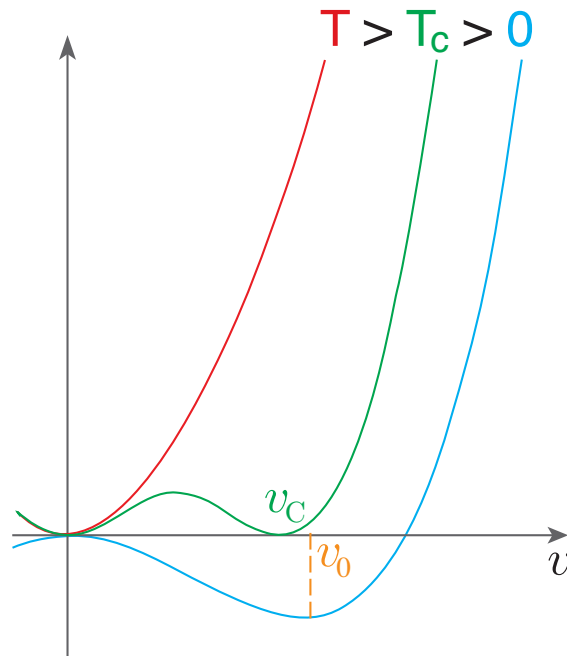
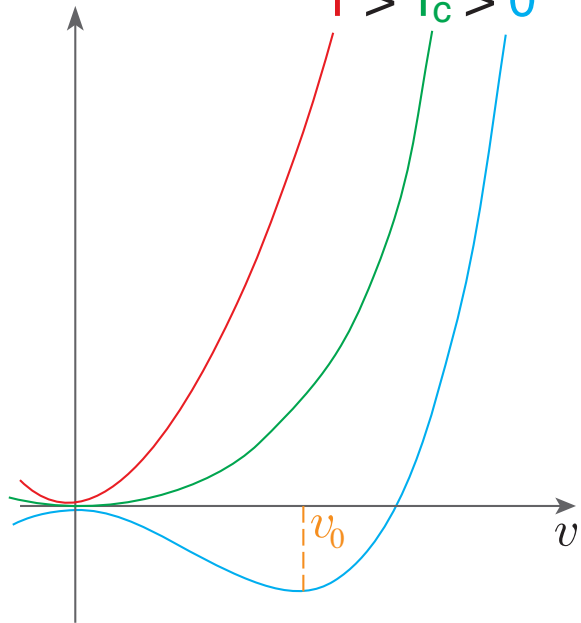
study of the EWPT

★ static properties  $\Leftarrow$  **effective potential** = free energy density

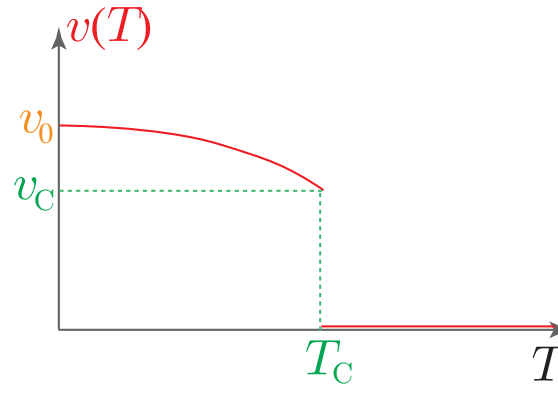
$$V_{\text{eff}}(\mathbf{v}; T) = -\frac{1}{V} T \log Z = -\frac{1}{V} \log \text{Tr} \left[ e^{-H/T} \right]_{\langle \phi \rangle = \mathbf{v}}$$

★ dynamics — formation and motion of the bubble wall when 1st order PT

$$V_{\text{eff}}(v;T) - V_{\text{eff}}(0;T)$$



2nd order PT



1st order PT

Minimal SM

order parameter:

$$\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \varphi \end{pmatrix}$$

$\therefore$  1st order EWPT



$$v_c \equiv \lim_{T \uparrow T_c} \varphi(T) \neq 0$$

## Minimal SM — perturbation at the 1-loop level

$$V_{\text{eff}}(\varphi; T) = -\frac{1}{2}\mu^2\varphi^2 + \frac{\lambda}{4}\varphi^4 + 2Bv_0^2\varphi^2 + B\varphi^4 \left[ \log\left(\frac{\varphi^2}{v_0^2}\right) - \frac{3}{2} \right] + \bar{V}(\varphi; T)$$

where  $B = \frac{3}{64\pi^2 v_0^4} (2m_W^4 + m_Z^4 - 4m_t^4),$

$$\bar{V}(\varphi; T) = \frac{T^4}{2\pi^2} [6I_B(a_W) + 3I_B(a_Z) - 6I_F(a_t)], \quad (a_A = m_A(\varphi)/T)$$

$$I_{B,F}(a^2) \equiv \int_0^\infty dx x^2 \log\left(1 \mp e^{-\sqrt{x^2+a^2}}\right).$$

high-temperature expansion [ $m/T \ll 1$ ]

$$I_B(a^2) = -\frac{\pi^4}{45} + \frac{\pi^2}{12}a^2 - \frac{\pi}{6}(a^2)^{3/2} - \frac{a^4}{16} \log \frac{\sqrt{a^2}}{4\pi} - \frac{a^4}{16} \left( \gamma_E - \frac{3}{4} \right) \frac{a^4}{2} + O(a^6)$$

$$I_F(a^2) = \frac{7\pi^4}{360} - \frac{\pi^2}{24}a^2 - \frac{a^4}{16} \log \frac{\sqrt{a^2}}{\pi} - \frac{a^4}{16} \left( \gamma_E - \frac{3}{4} \right) + O(a^6)$$

For  $T > m_W, m_Z, m_t$ ,

$$V_{\text{eff}}(\varphi; T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4$$

where

$$D = \frac{1}{8v_0^2}(2m_W^2 + m_Z^2 + 2m_t^2), \quad E = \frac{1}{4\pi v_0^3}(2m_W^3 + m_Z^3) \sim 10^{-2}$$

$$\lambda_T = \lambda - \frac{3}{16\pi^2 v_0^4} \left( 2m_W^4 \log \frac{m_W^2}{\alpha_B T^2} + m_Z^4 \log \frac{m_Z^2}{\alpha_B T^2} - 4m_t^4 \log \frac{m_t^2}{\alpha_F T^2} \right)$$

$$T_0^2 = \frac{1}{2D}(\mu^2 - 4Bv_0^2), \quad \log \alpha_{F(B)} = 2 \log(4)\pi - 2\gamma_E$$

At  $T_C$ ,  $\exists$  degenerate minima:  $\varphi_C = \frac{2ET_C}{\lambda_{T_C}}$

$$\Gamma_{\text{sph}}^{(b)}/T_C^3 < H(T_C) \iff \frac{\varphi_C}{T_C} \gtrsim 1 \implies \text{upper bound on } \lambda \quad [m_H = \sqrt{2}\lambda v_0]$$

$$m_H \lesssim 46 \text{ GeV}$$

$\implies$  MSM is excluded



## ★ Monte Carlo simulations

[MSM]

effective fermion mass :  $m_f(T) \sim O(T) \leftarrow$  nonzero modes

$\therefore$  simulation only with the bosons

QFT on the lattice  $\left\{ \begin{array}{l} \text{scalar fields: } \phi(x) \text{ on the sites} \\ \text{gauge fields: } U_\mu(x) \text{ on the links} \end{array} \right.$

$$Z = \int [d\phi dU_\mu] \exp \{-S_E[\phi, U_\mu]\}$$

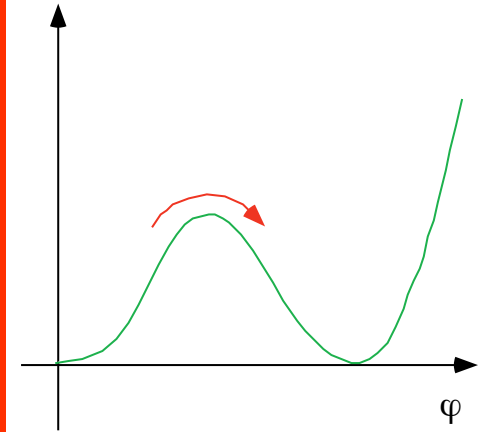
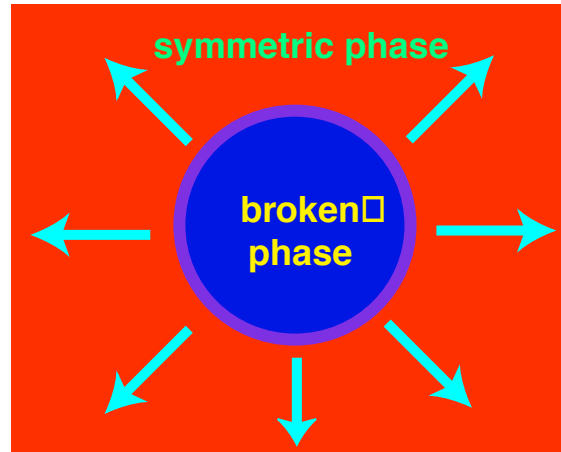
- 3-dim.  $SU(2)$  system with a Higgs doublet and a triplet      time-component of  $U_\mu$   
[Laine & Rummukainen, hep-lat/9809045]
- 4-dim.  $SU(2)$  system with a Higgs doublet      [Csikor, hep-lat/9910354]  
EWPT is first order for  $m_h < 66.5 \pm 1.4 \text{ GeV}$

Both the simulations found end-point of EWPT at

$$m_h = \left\{ \begin{array}{l} 72.3 \pm 0.7 \text{ GeV} \\ 72.1 \pm 1.4 \text{ GeV} \end{array} \right. \Rightarrow \boxed{\text{no PT (cross-over) in the MSM !}}$$

★ Dynamics of the phase transition

first-order EWPT accompanying  
bubble nucleation/growth



nucleation rate per unit time and unit volume:  $I(T) = I_0 e^{-\Delta F(T)/T}$   
where

$$\Delta F(T) = \frac{4\pi}{3} r^3 [p_s(T) - p_b(T)] + 4\pi r^2 \sigma,$$

$$p_s(T) = -V_{\text{eff}}(0; T), \quad p_b(T) = -V_{\text{eff}}(\varphi(T); T)$$

supercooling  $\longrightarrow p_s(T) < p_b(T)$

$\sigma \simeq \int dz (d\varphi/dz)^2$  : surface energy density

radius of the critical bubble :  $r_*(T) = \frac{2\sigma}{p_b(T) - p_s(T)}$

## How the EWPT proceeds ?

[Carrington and Kapsta, P.R.D47('93)]

$f(t)$  : fraction of space converted to the broken phase

$$f(t) = \int_{t_C}^t dt' I(T(t')) [1 - f(t')] V(t', t)$$

where

$V(t', t)$  : volume of a bubble at  $t$  which was nucleated at  $t'$

$$V(t', t) = \frac{4\pi}{3} \left[ r_*(T(t')) + \int_{t'}^t dt'' v(T(t'')) \right]^3$$

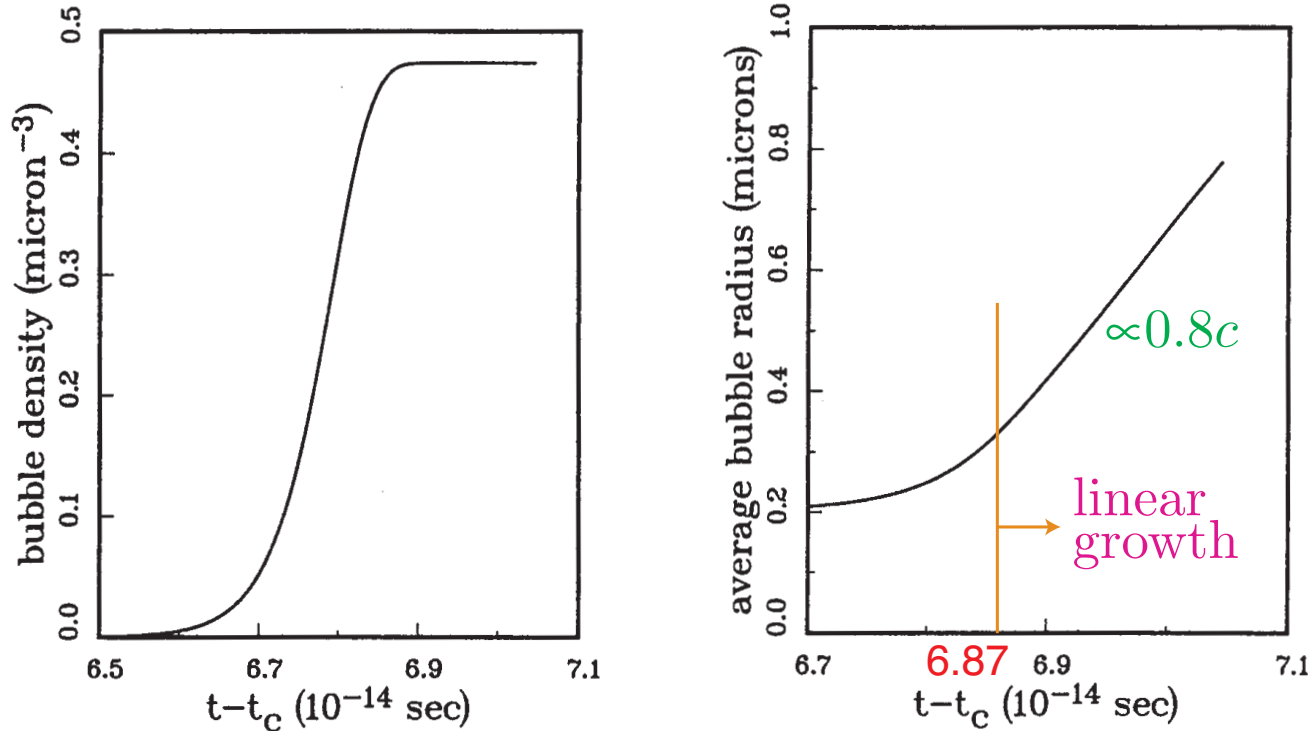
$T = T(t) \iff \rho = (\pi^2/30)g_*T^4 \propto R^{-4}$  for RD universe

$v(T)$  : wall velocity

- one-loop  $V_{\text{eff}}$  of MSM with  $m_H = 60\text{GeV}$  and  $m_t = 120\text{GeV}$

At  $t = 6.5 \times 10^{-14}$  sec, bubbles began to nucleate.

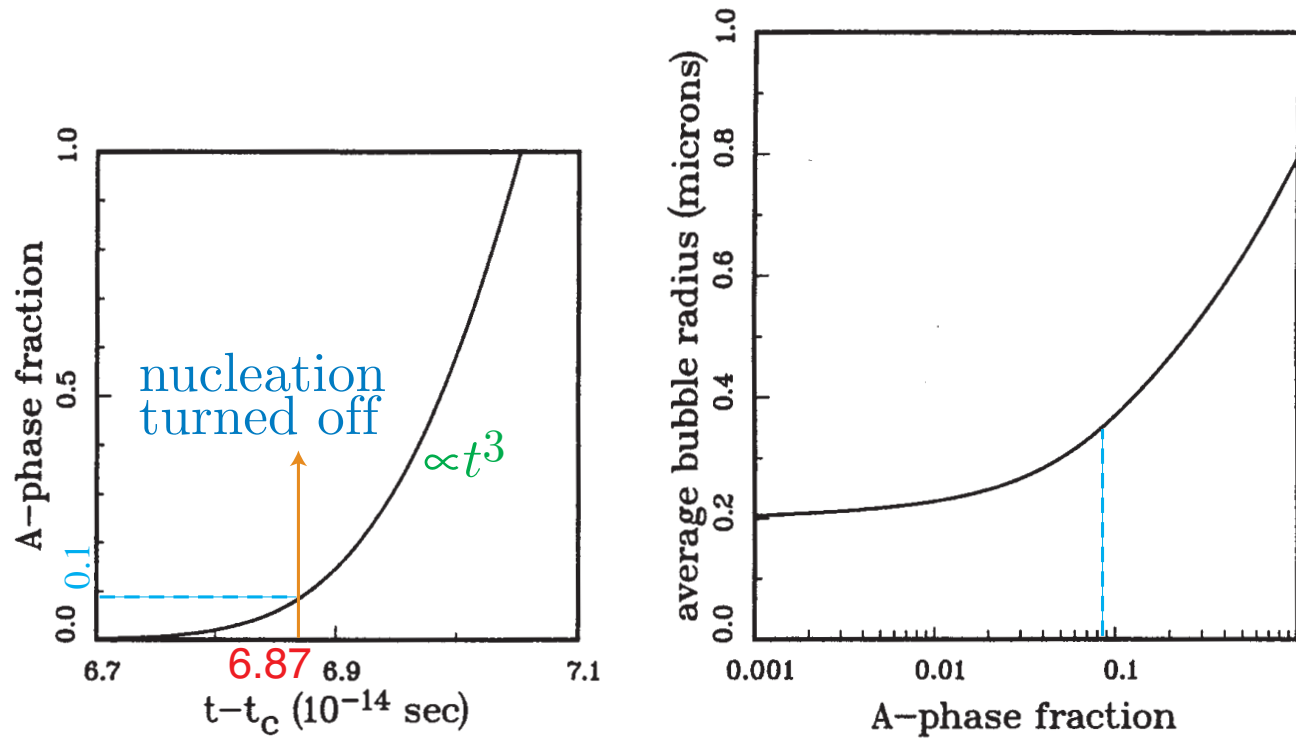
[A characteristic time scale of the EW processes is  $O(10^{-26})\text{sec}$ .]



horizon size :  $H^{-1} \simeq 7.1 \times 10^{12} \text{ GeV}^{-1} = 0.14 \text{ cm}$

$r = 0.3\mu\text{m} \Rightarrow \#(\text{bubbles within a horizon}) \simeq 3 \times 10^{11}$

very small supercooling :  $(T_C - T_N)/T_C \simeq 2.5 \times 10^{-4}$



weakly first order  $\iff$  small  $v_C$  and/or lower barrier height

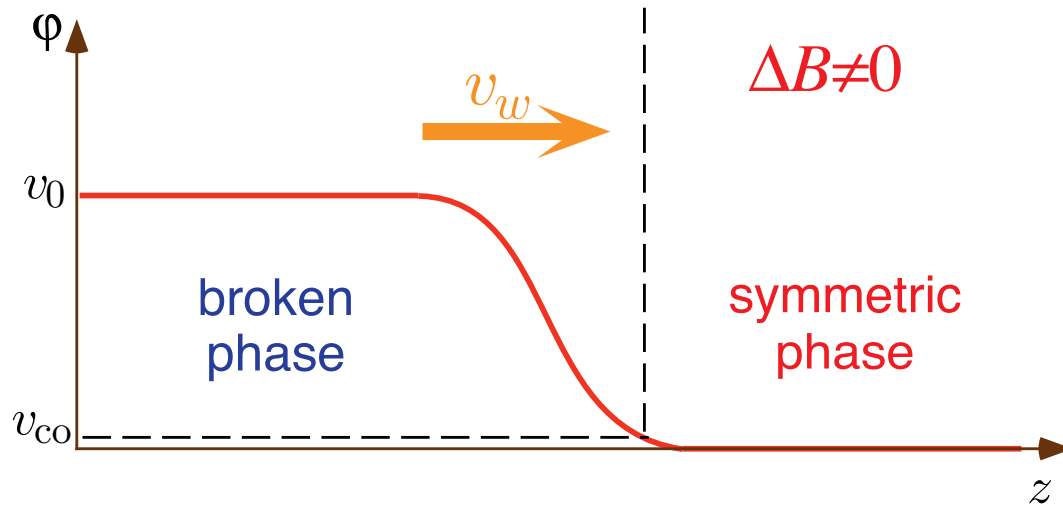
$\implies$  { nucleation dominance over growth  
 thick bubble wall  
 large fluctuation between the two phases

## Mechanism of the baryogenesis

$$\bar{t}_s \simeq 0.1\text{GeV}^{-1} \ll \bar{t}_{EW} \simeq 1\text{GeV}^{-1} \ll \bar{t}_{\text{sph}} \simeq 10^5\text{GeV}^{-1} \ll H^{-1} \simeq 10^{14}\text{GeV}^{-1}$$

EW bubble wall motion:  $t_{\text{wall}} = \frac{l_w}{v_w} = \frac{(1 - 40)/T}{0.1 - 0.9} = (0.01 - 4)\text{GeV}^{-1}$

1. All the particles are in *kinetic equilibrium at the same temperature*, because of  $H^{-1} \gg \bar{t}_{EW}$ , far from the bubble wall.
2. Since  $\lambda_Y > \lambda_{EW} \gg l_w$ , the leptons and some of the quarks propagate almost freely before and after the scattering off the bubble wall.
3. Because of  $t_{\text{wall}} \ll \bar{t}_{\text{sph}}$ , the sphaleron process is *out of chemical equilibrium* near the bubble wall.



$$v_{co} \simeq 0.01v_0 \Leftarrow E_{\text{sph}}/T_C \simeq 1$$

**bubble wall**  $\Leftarrow$  classical config. of the gauge-Higgs system

- interactions between the particles and the bubble wall
- accumulation of **chiral charge** in the **symmetric phase**
  - $\Downarrow$
  - generation of baryon number through **sphaleron process**
  - $\Downarrow$
  - decoupling of sphaleron process** in the broken phase

2 scenarios:  $\left\{ \begin{array}{l} \circ \text{spontaneous baryogenesis} + \text{diffusion} \quad \text{classical, adiabatic} \\ \bullet \text{charge transport scenario} \quad \text{quantum mechanical, nonlocal} \end{array} \right.$

Both need CP violation other than KM matrix  $\Rightarrow$  extension of the MSM  
2HDM, MSSM, ...

★ Charge transport mechanism

CP violation in the Higgs sector or in the mass matrix of  $\tilde{\chi}, \tilde{q}$   
[spacetime-dependent CP violation]



difference in reflections of chiral fermions and antifermions



net chiral charge flux into the symmetric phase

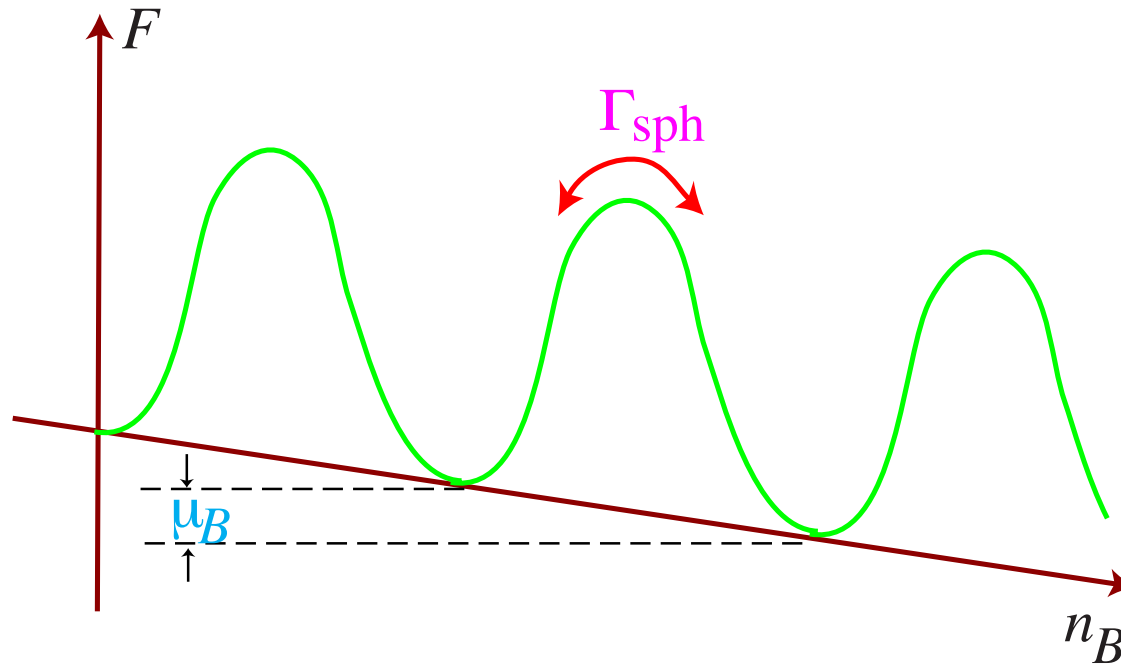


change of distribution functions by the chiral charge  
with the sphaleron process in equilibrium



$v_w \simeq \text{const.} \Rightarrow$  stationary nonequilibrium : bias on free energy along  $B$

$$\dot{n}_B \simeq -\frac{\mu_B \Gamma_{\text{sph}}}{T}$$



According to the relations among the chemical potentials (sphaleron is excluded),

$$\mu_B = \frac{Y}{2(m + 5/3)T^2}$$

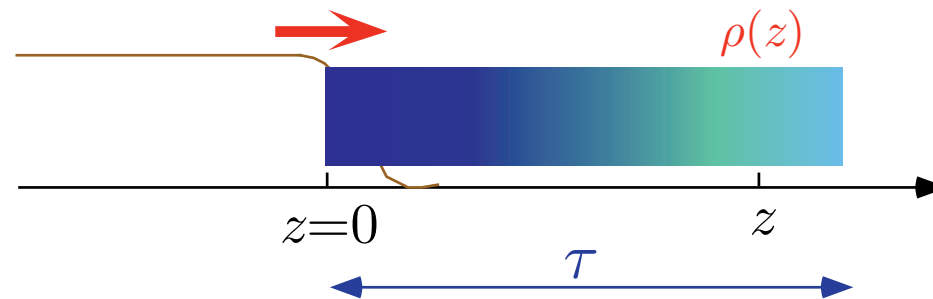
$m = \#(\text{Higgs doublets})$

## BAU by electroweak baryogenesis

$$n_B = -\frac{\Gamma_{\text{sph}}}{T} \int dt \mu_B = -\frac{\Gamma_{\text{sph}}}{2(m + 5/3)T^3} \int dt Y$$

where

$$\int dt Y = \int_{-\infty}^{z/v_w} dt \rho_Y(z - v_w t) = \frac{1}{v_w} \int_0^{\infty} dz \rho_Y(z) \simeq \frac{F_Y \tau}{v_w}$$



$\tau$  = transport time within which the scattered fermions are captured by the wall

$$\frac{n_B}{s} \simeq \mathcal{N} \frac{100}{\pi^2 g_*} \cdot \kappa \alpha_W^4 \cdot \frac{F_Y}{v_w T^3} \cdot \tau T$$

$$\mathcal{N} \sim O(1), \quad \tau T \simeq \begin{cases} 1 & \text{for quarks} \\ 10^2 \sim 10^3 & \text{for leptons} \end{cases}$$

MC simulation  $\implies$  forward scattering enhanced :

for top quark  $\tau T \simeq 10 \sim 10^3$  max. at  $v_w \simeq 1/\sqrt{3}$

for this optimal case

$$\frac{n_B}{s} \simeq 10^{-3} \cdot \frac{F_Y}{v_w T^3}$$

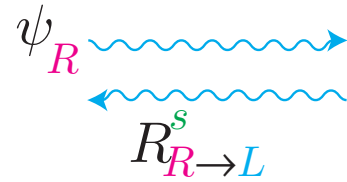
$F_Y/(v_w T^3) \sim O(10^{-7})$  would be sufficient to explain the BAU.

## Calculation of the chiral charge flux

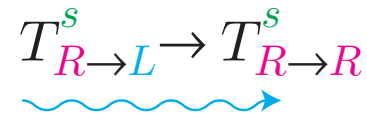
$$i\partial\psi(x) - m(x)P_R\psi(x) - m^*(x)P_L\psi(x) = 0$$

where  $-f\langle\phi(x)\rangle = m(x) \in \mathbf{C}$  through the Yukawa int.

symmetric phase



broken phase



$Q_{L(R)}^i$  : charge of a L(R)-handed fermion of species  $i$

$R_{R \rightarrow L}^s$  : reflection coeff. for the R-handed fermion incident from the symmetric phase region

$\bar{R}_{R \rightarrow L}^s$  : the same as above for the R-handed antifermion

(injected charge into symmetric phase) brought by the fermions and antifermions in the **symmetric phase** :

$$\begin{aligned} \Delta Q_i^s = & [(Q_R^i - Q_L^i)R^s_{L \rightarrow R} + (-Q_L^i + Q_R^i)\bar{R}^s_{R \rightarrow L} \\ & + (-Q_L^i)(T^s_{L \rightarrow L} + T^s_{L \rightarrow R}) - (-Q_R^i)(\bar{T}^s_{R \rightarrow L} + \bar{T}^s_{R \rightarrow R})]f^s_{Li} \\ & + [(Q_L^i - Q_R^i)R^s_{R \rightarrow L} + (-Q_R^i + Q_L^i)\bar{R}^s_{L \rightarrow R} \\ & + (-Q_R^i)(T^s_{R \rightarrow L} + T^s_{R \rightarrow R}) - (-Q_L^i)(\bar{T}^s_{L \rightarrow L} + \bar{T}^s_{L \rightarrow R})]f^s_{Ri} \end{aligned}$$

the same brought by transmission from the **broken phase** :

$$\begin{aligned} \Delta Q_i^b = & Q_L^i(T^b_{L \rightarrow L}f^b_{Li} + T^b_{R \rightarrow L}f^b_{Ri}) + Q_R^i(T^b_{L \rightarrow R}f^b_{Li} + T^b_{R \rightarrow R}f^b_{Ri}) \\ & + (-Q_L^i)(\bar{T}^b_{R \rightarrow L}f^b_{Li} + \bar{T}^b_{L \rightarrow L}f^b_{Ri}) + (-Q_R^i)(\bar{T}^b_{R \rightarrow R}f^b_{Li} + \bar{T}^b_{L \rightarrow R}f^b_{Ri}) \end{aligned}$$

by use of

unitarity:  $R^s_{L \rightarrow R} + T^s_{L \rightarrow L} + T^s_{L \rightarrow R} = 1,$  etc.

reciprocity:  $T^s_{R \rightarrow L} + T^s_{R \rightarrow R} = T^b_{L \rightarrow L} + T^b_{R \rightarrow L},$  etc.

$$f_{iL}^{s(b)} = f_{iR}^{s(b)} \equiv f_i^{s(b)}$$

$$\Delta Q^s_i + \Delta Q^b_i = (Q_L^i - Q_R^i)(f_i^s - f_i^b)\Delta R$$

where

$$\Delta R \equiv R^s_{R \rightarrow L} - \bar{R}^s_{R \rightarrow L}$$

- which depends on
- profile of the bubble wall      wall thickness, height, CP phase
  - momentum of the incident particle

total flux injected into the *symmetric phase* region

$$F^i_Q = \frac{Q_L^i - Q_R^i}{4\pi^2\gamma} \int_{m_0}^{\infty} dp_L \int_0^{\infty} dp_T p_T [f_i^s(p_L, p_T) - f_i^b(-p_L, p_T)] \Delta R\left(\frac{m_0}{a}, \frac{p_L}{a}\right)$$

$$f_i^s(p_L, p_T) = \frac{p_L}{E} \frac{1}{\exp[\gamma(E - v_w p_L)/T] + 1}$$

$$f_i^b(-p_L, p_T) = \frac{p_L}{E} \frac{1}{\exp[\gamma(E + v_w \sqrt{p_L^2 - m_0^2})/T] + 1}$$

$1/a =$  wall width,  $m_0 =$  mass in the broken phase,  $E = \sqrt{p_L^2 + p_T^2}$

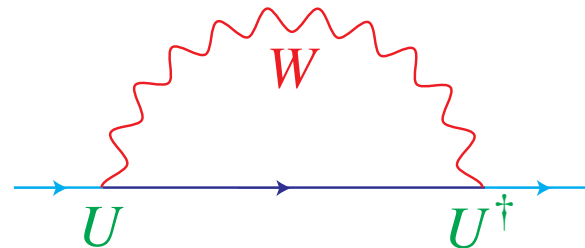
available charge :  $Q_L - Q_R \neq 0$  }  $\implies$   $Y, I_3$   
 conserved in the symmetric phase

N.B. For  $B$ , no  $F_B$  is generated, since it is vectorlike.

CP violation effective for  $\Delta R$

- Minimal SM — KM phase

dispersion relation of the fermion  $\sim O(\alpha_W)$  [Farrar and Shaposhnikov, PRD, '94]



— decoherence by QCD effects (short range)  
 [Gavela, et al., NPB '94]

- CP violation in mass or mass matrix

*tree-level* quantum scattering by the bubble wall

★ relative phase of 2 Higgs doublets  $\Rightarrow m(x) = -g |\phi(x)| e^{i\theta(x)}$

★ relative phases of the complex parameters in Supersymmetric SM

$\Rightarrow$  mass matrices of chargino, neutralino, sfermions

$$M_{\chi^\pm} = \begin{pmatrix} M_2 & -\frac{i}{\sqrt{2}}g_2 v_u e^{-i\theta} \\ -\frac{i}{\sqrt{2}}g_2 v_d & -\mu \end{pmatrix}$$

*x*-dependent  $v_d$  and  $v_u \Rightarrow$  effectively *x*-dependent phases



★ **Example**

[Nelson et al., NPB, '92]

$$m(z) = m_0 \frac{1 + \tanh(az)}{2} \exp\left(-i\pi \frac{1 - \tanh(az)}{2}\right)$$

— no CP violation in the broken phase [ $z \sim \infty$ ]

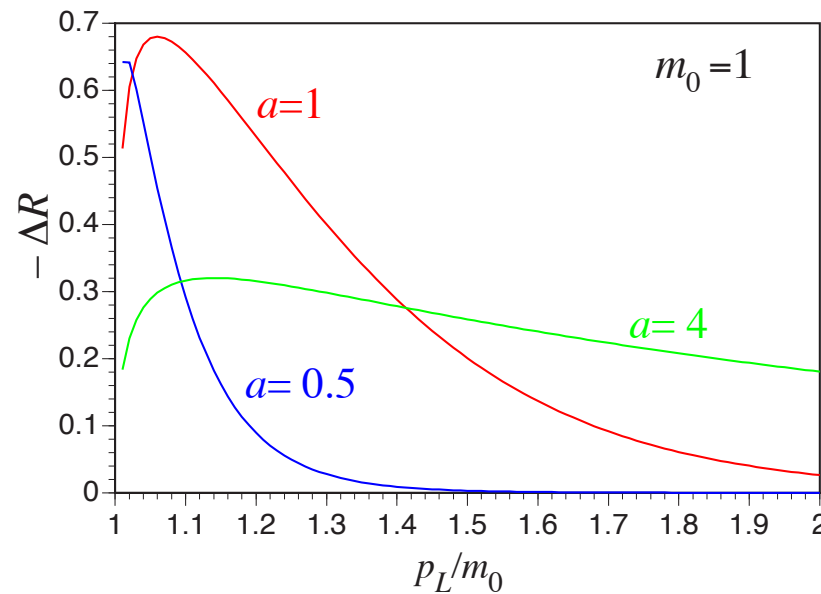
•  $\Delta R \equiv R^s_{R \rightarrow L} - \bar{R}^s_{R \rightarrow L}$

[FKOTT, PRD'94; PTP'96]

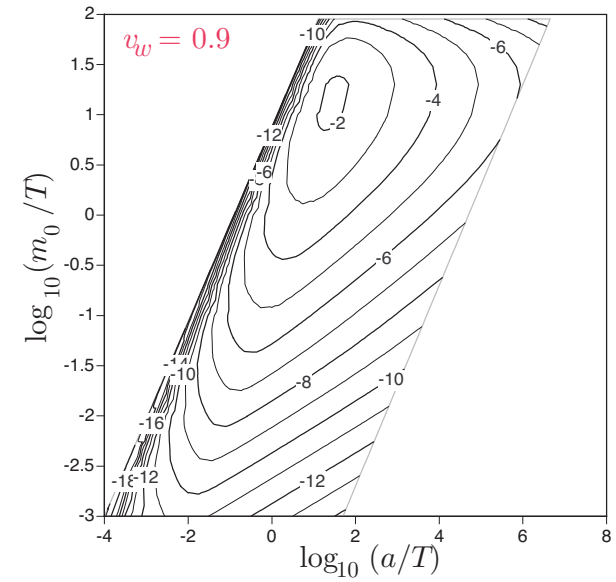
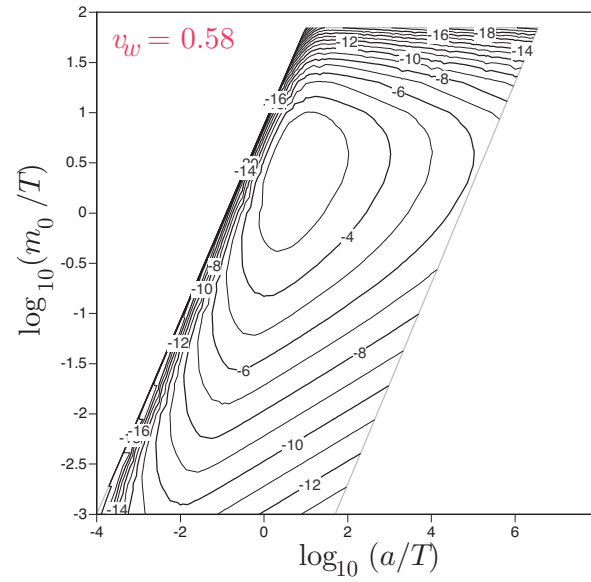
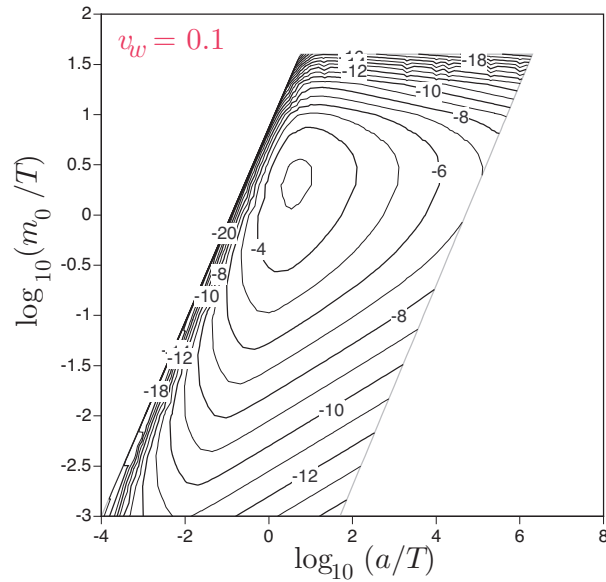
wall width  $\simeq$  wave length of the carrier  $\Rightarrow \Delta R \sim O(1)$



stronger Yukawa coupling does *not* always implies larger flux



- chiral charge flux normalized as  $\frac{F_Q}{T^3(Q_L - Q_R)}$  [dimensionless] at  $T = 100\text{GeV}$



$$\frac{n_B}{s} \simeq \mathcal{N} \frac{100}{\pi^2 g_*} \cdot \kappa \alpha_W^4 \cdot \frac{F_Y}{v_w T^3} \cdot \tau T \simeq 10^{-3} \cdot \frac{F_Y}{v_w T^3}$$

for an optimal case

# EW baryogenesis in the MSSM

- EW Phase Transition

3 order parameters:  $\langle \Phi_d \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v_1 \\ 0 \end{pmatrix}, \quad \langle \Phi_u \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 + iv_3 \end{pmatrix}$

- CP Violation

complex parameters:  $\mu, M_{3,2,1}, A, \mu B = m_3^2$

$v_3 \neq 0$  —  $v_3 = 0$  at the tree level

- sphaleron solution

{ 2HDM  
squarks vs sphaleron  
NMSSM

[Peccei, et al, PLB '91]  
[Moreno, et al, PLB '97]  
[KF, et al, in progress]

## ★ Electroweak phase transition

light stop scenario

[de Carlos & Espinosa, NPB '97]

$$\mathcal{M}_{\tilde{t}}^2 = \begin{pmatrix} m_{\tilde{t}_L}^2 + \left(\frac{g_1^2}{24} - \frac{g_2^2}{8}\right)(v_u^2 - v_d^2) + \frac{y_t^2}{2}v_u^2 & \frac{y_t}{\sqrt{2}}(\mu v_d + A(v_2 - iv_3)) \\ * & m_{\tilde{t}_R}^2 - \frac{g_1^2}{6}(v_u^2 - v_d^2) + \frac{y_t^2}{2}v_u^2 \end{pmatrix}$$

$m_{\tilde{t}_L}^2 = 0$  or  $m_{\tilde{t}_R}^2 = 0 \implies$  smaller eigenvalue:  $m_{\tilde{t}_1}^2 \sim O(v^2)$

$\therefore$  high- $T$  expansion

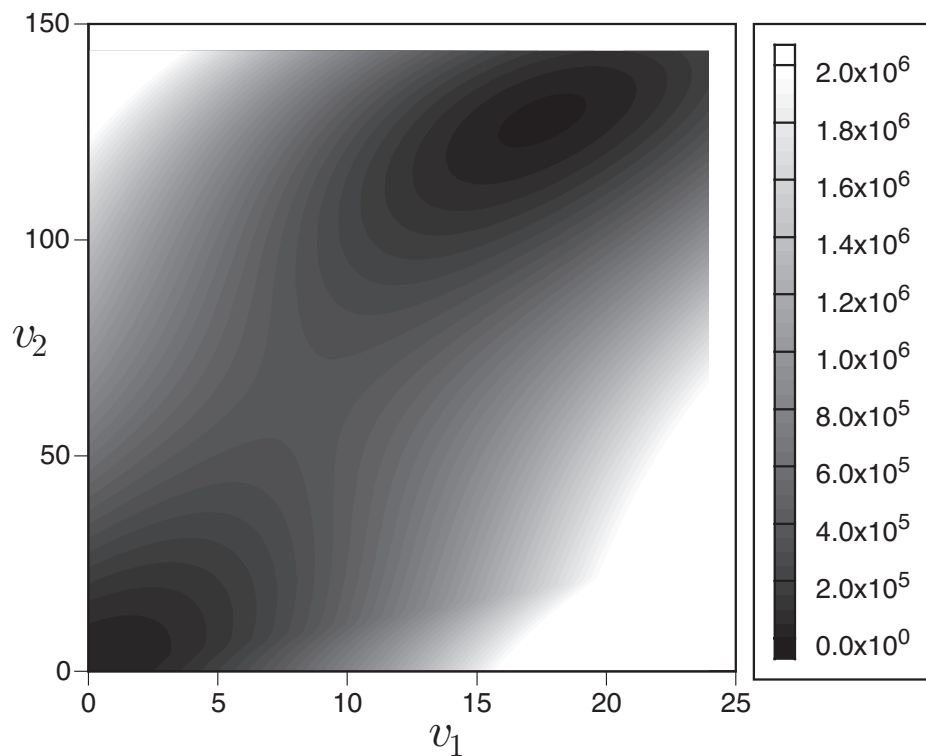
$$\bar{V}_{\tilde{t}}(\mathbf{v}; T) \implies -\frac{T}{6\pi}(m_{\tilde{t}_1}^2)^{3/2} \sim T v^3$$

$\longrightarrow$  stronger 1st order PT

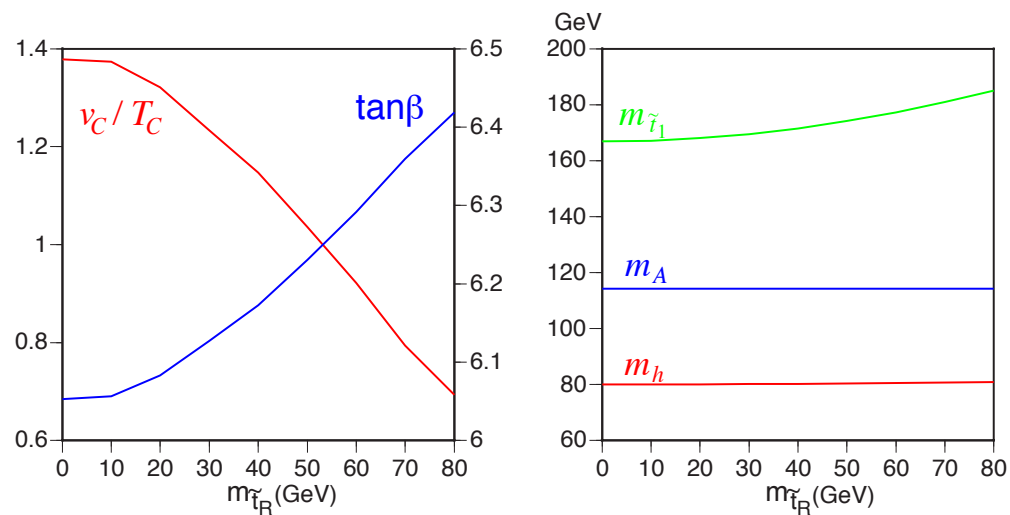
effective for larger  $y_t$  — smaller  $\tan\beta$

An example:  $\tan \beta = 6$ ,  $m_h = 82.3\text{GeV}$ ,  $m_A = 118\text{GeV}$ ,  $m_{\tilde{t}_1} = 168\text{GeV}$   
 $T_C = 93.4\text{GeV}$ ,  $v_C = 129\text{GeV}$

[KF, PTP101]



$V_{\text{eff}}(v_1, v_2, v_3 = 0; T_C)$



$m_{t_R}$ -dependence ( $\tan \beta = 6$ )

★ Lattice MC studies

- 3d reduced model

[Laine et al. hep-lat/9809045]

strong 1st order for  $m_{\tilde{t}_1} \lesssim m_t$  and  $m_h \leq 110\text{GeV}$

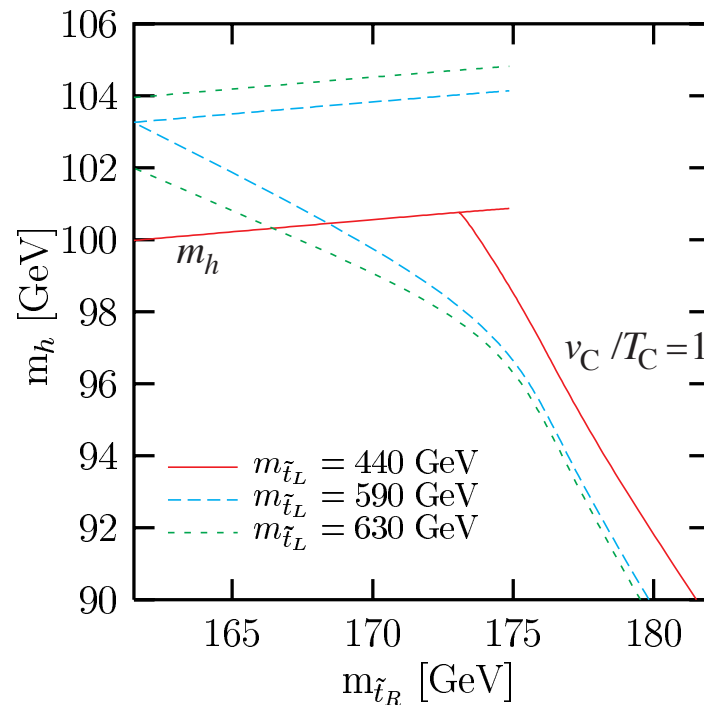
- 4d model

[Csikor, et al. hep-lat/0001087]

with  $SU(3)$ ,  $SU(2)$  gauge bosons, 2 Higgs doublets, stops, sbottoms

$A_{t,b} = 0$ ,  $\tan \beta \simeq 6$

→ agreement with the perturbation theory within the errors



$m_A = 500\text{ GeV}$

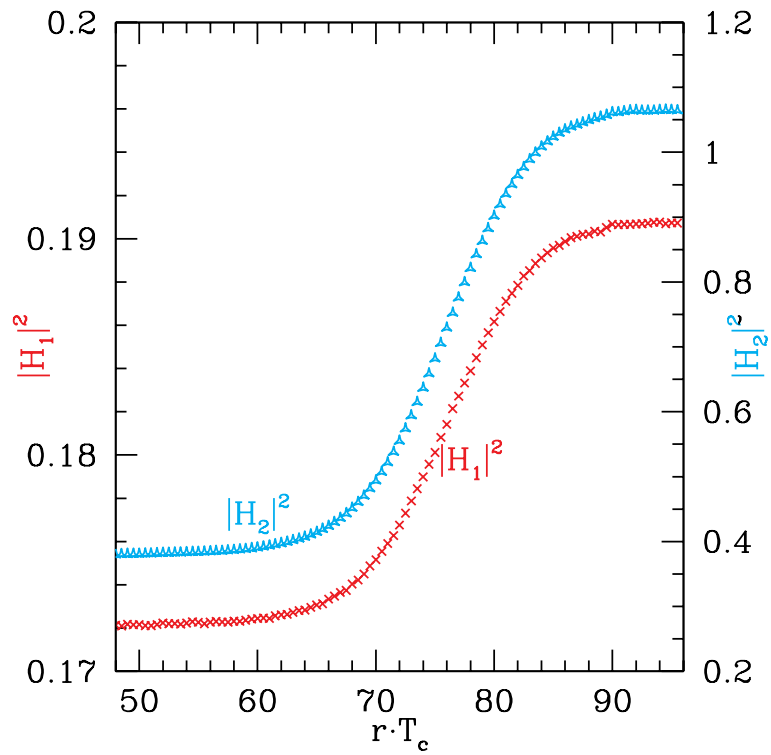
$v_C/T_C > 1$

below the steeper lines



max.  $m_h = 103 \pm 4\text{ GeV}$

for  $m_{\tilde{t}_L} \simeq 560\text{ GeV}$

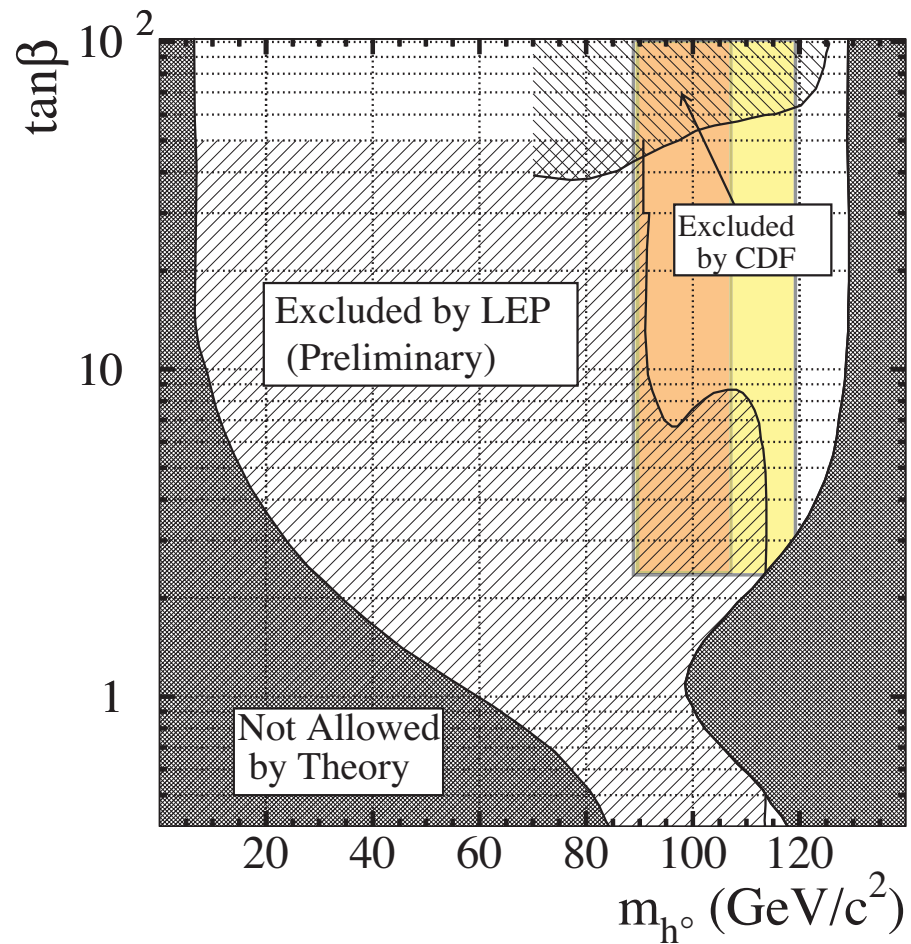


bubble-wall profile

$$\Delta\beta = 0.0061 \pm 0.0003$$

$\Rightarrow \beta \simeq \text{const.}$

$$\text{wall width} \simeq \frac{11}{T_C}$$



[PDG,  
<http://ccwww.kek.jp/pdg/>]

light stop:  $m_{t_R} = 0$

negative soft mass<sup>2</sup>:  $m_{t_R}^2 > -(65\text{GeV})^2$

[Laine & Rummukainen, NPB597]



## ★ CP Violation

- ★ relative phases of  $\mu, M_2, M_1, A_t$   
chargino, neutralino, stop transport [Huet & Nelson, PRD '96; Aoki, et al. PTP '97]
- ★ relative phase  $\theta = \theta_1 - \theta_2$  of the two Higgs doublets  
quarks and leptons  $\leftarrow$  Yukawa coupl.  $\propto \rho_i e^{i\theta_i}$   
chargino, neutralino, stop mass matrix  
[Nelson et al. NPB '92; FKOTT, PRD '94, PTP '96]

$\theta$  is induced by the loops of SUSY particle.

$$\uparrow \leftarrow \text{Arg}(\mu M_2), \text{Arg}(\mu M_1), \text{Arg}(\mu A_t)$$

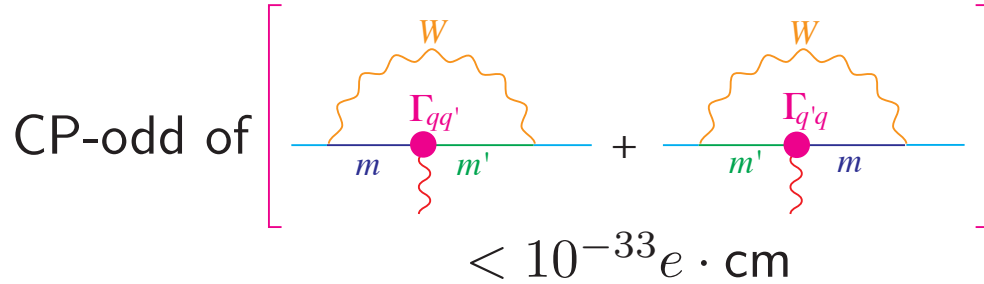
minimum of  $V_{\text{eff}}(\rho_i, \theta; T = 0)$

CP violation at  $T = 0$  is constrained by experiments (B factory, nEDM, etc)

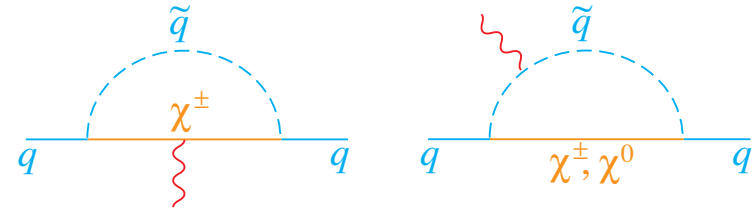
CP violation at  $T_C$  near the bubble wall is relevant to baryogenesis

bounds from the EDM :  $|d_n| < 0.63 \times 10^{-25} e \cdot \text{cm}$  [Kizukuri & Oshimo, PRD '92]

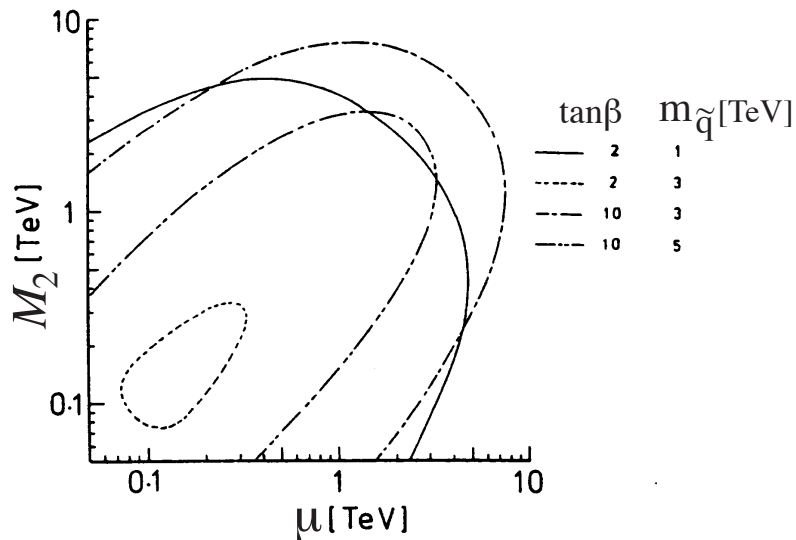
MSM contribution:



MSSM contribution:



... etc.



$\theta + \delta_\mu + \delta_2 = \pi/4$   
 $\text{Arg}A = \pi/4$

inside is excluded

FIG. 4. The parameter regions compatible with the present experimental upper bound on the neutron EDM.

- $\bullet \theta + \delta_\mu + \delta_2 = O(1) \implies m_{\tilde{q}}, m_{\tilde{l}} \gtrsim 10\text{TeV}$
- $\bullet m_{\tilde{q}}, m_{\tilde{l}} \lesssim 1\text{TeV} \implies \theta + \delta_\mu + \delta_2 \lesssim 10^{-3}$

CP violation relevant to Baryogenesis —  $\theta(x)$  in the bubble wall

Eqs. of motion for  $(\rho_i(x), \theta(x))$  with  $V_{\text{eff}}(\rho_i, \theta; T_C)$

with B.C. determined by the min. of  $V_{\text{eff}}(T_C)$

$\rho(x)$ : 0 (sym. phase)  $\longrightarrow$   $v_C$  (br. phase) — kink-like

$\theta(x)$ :  $-\text{Arg}(m_3^2)$  (sym. phase)  $\longrightarrow$   $\theta_C$  (br. phase)  $\stackrel{\text{loop}}{\Leftarrow}$  explicit CP violation

bubble wall  $\sim$  macroscopic, static  $\rightarrow$  1d system  $\Rightarrow$  numerical solution

### possible CP violations

- $\theta(x)$  near the wall  $\sim O(\theta_C)$
- transitional CP violation —  $\theta(x) = O(1)$  near the wall, even if  $\theta_C \ll 1$

Suppose that at  $T \simeq T_C$ , without explicit CP violation,

$$[\theta = \theta_1 - \theta_2]$$

$$V_{\text{eff}}(\rho_i, \theta)$$

$$\begin{aligned}
 &= \frac{1}{2}\bar{m}_1^2\rho_1^2 + \frac{1}{2}\bar{m}_2^2\rho_2^2 - \bar{m}_3^2\rho_1\rho_2 \cos \theta + \frac{\lambda_1}{8}\rho_1^4 + \frac{\lambda_2}{8}\rho_2^4 \\
 &+ \frac{\lambda_3 + \lambda_4}{4}\rho_1^2\rho_2^2 + \frac{\lambda_5}{4}\rho_1^2\rho_2^2 \cos 2\theta - \frac{1}{2}(\lambda_6\rho_1^2 + \lambda_7\rho_2^2)\rho_1\rho_2 \cos \theta \\
 &- [A\rho_1^3 + \rho_1^2\rho_2(B_0 + B_1 \cos \theta + B_2 \cos 2\theta) + \rho_1\rho_2^2(C_0 + C_1 \cos \theta + C_2 \cos 2\theta) + D\rho_2^3] \\
 &= \left[ \frac{\lambda_5}{2}\rho_1^2\rho_2^2 - 2(B_2\rho_1^2\rho_2 + C_2\rho_1\rho_2^2) \right] \left[ \cos \theta - \frac{2\bar{m}_3^2 + \lambda_6\rho_1^2 + \lambda_7\rho_2^2 + 2(B_1\rho_1 + C_1\rho_2)}{2\lambda_5\rho_1\rho_2 - 8(B_2\rho_1 + C_2\rho_2)} \right]^2 \\
 &\quad + \theta\text{-independent terms}
 \end{aligned}$$

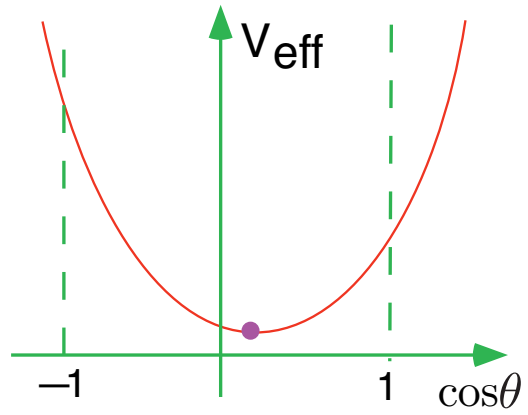
where all the parameters are real

conditions for spontaneous CP violation for a given  $(\rho_1, \rho_2)$

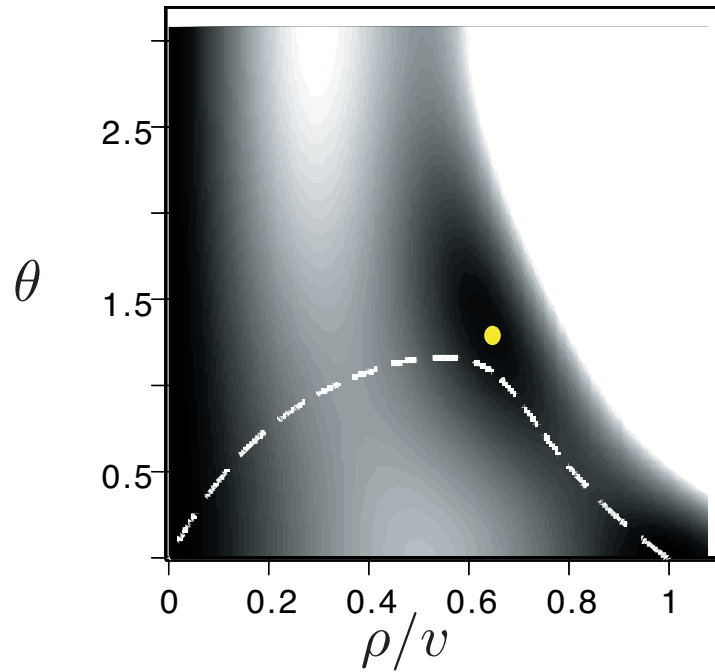
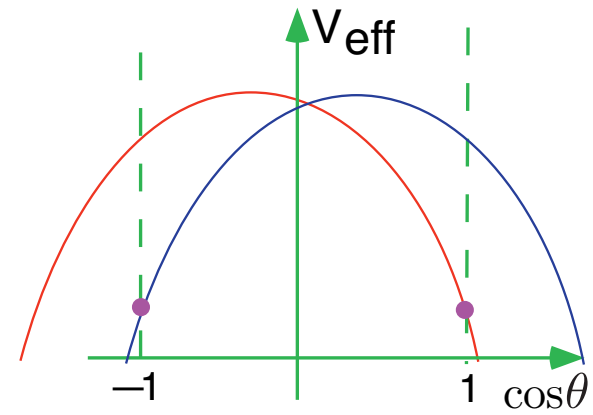
$$F(\rho_1, \rho_2) \equiv \frac{\lambda_5}{2} \rho_1^2 \rho_2^2 - 2(B_2 \rho_1^2 \rho_2 + C_2 \rho_1 \rho_2^2) > 0,$$

$$-1 < G(\rho_1, \rho_2) \equiv \frac{2\bar{m}_3^2 + \lambda_6 \rho_1^2 + \lambda_7 \rho_2^2 + 2(B_1 \rho_1 + C_1 \rho_2)}{2\lambda_5 \rho_1 \rho_2 - 8(B_2 \rho_1 + C_2 \rho_2)} < 1$$

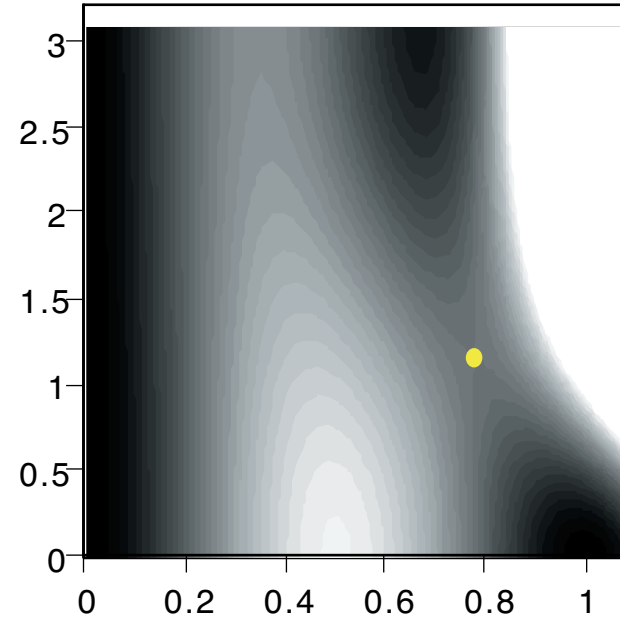
$$F(\rho_1, \rho_2) > 0$$



$$F(\rho_1, \rho_2) < 0$$



CP-violating **local min.**



CP-violating **saddle point**

## An Example

[KF, Otsuki & Toyoda, PTP '99]

### input parameters

$\tan \beta_0$	$m_3^2$	$\mu$	$A_t$	$M_2 = M_1$	$m_{\tilde{t}_L}$	$m_{\tilde{t}_R}$
6	8110 GeV <sup>2</sup>	-500 GeV	60 GeV	500 GeV	400 GeV	0

### mass spectrum

$m_h$	$m_A$	$m_H$	$m_{\tilde{t}_1}$	$m_{\chi_1^\pm}$	$m_{\chi_1^0}$
82.28 GeV	117.9 GeV	124.0 GeV	167.8 GeV	457.6 GeV	449.8 GeV

results:  $T_C = 93.4$  GeV,  $v_C = 129.17$  GeV,  $\tan \beta = 7.292$ ,

inverse wall width:  $a = 13.23$  GeV

$\implies$  BAU:  $\frac{n_B}{s} \sim 10^{-(12-10)}$

$[v_w = 0.1, \text{Arg}(m_3^2) = 10^{-3}]$

—  $\tau$ -dominant

EWPT in the light-stop scenario [ $m_{\tilde{t}_R} = 10\text{GeV}$ ]

$$\text{Im}(\mu A_t e^{i\theta}) \neq 0 \Rightarrow \begin{cases} \triangleright \text{scalar-pseudoscalar mixing} \\ \triangleright \text{induces } \delta = \text{Arg}(m_3^2) \\ \bullet \text{ weakens the EWPT} \end{cases} \quad [\text{Carena, et al., NPB586}]$$

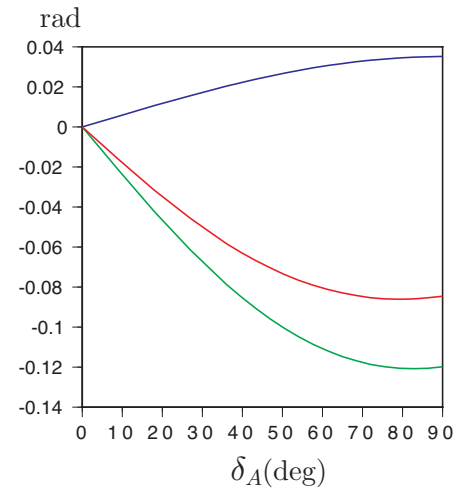
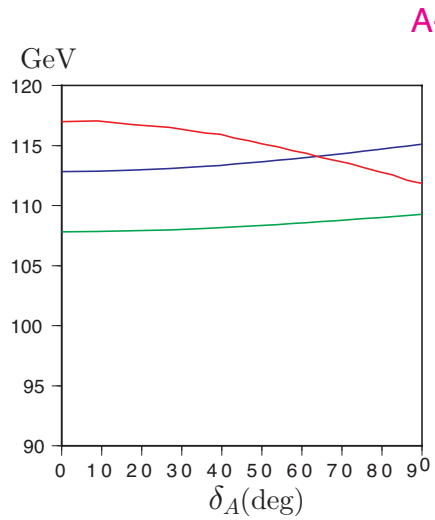
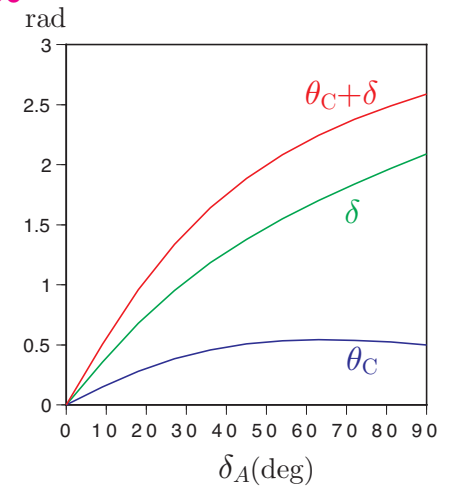
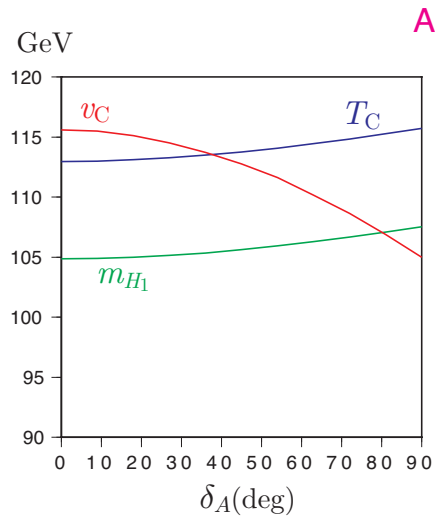
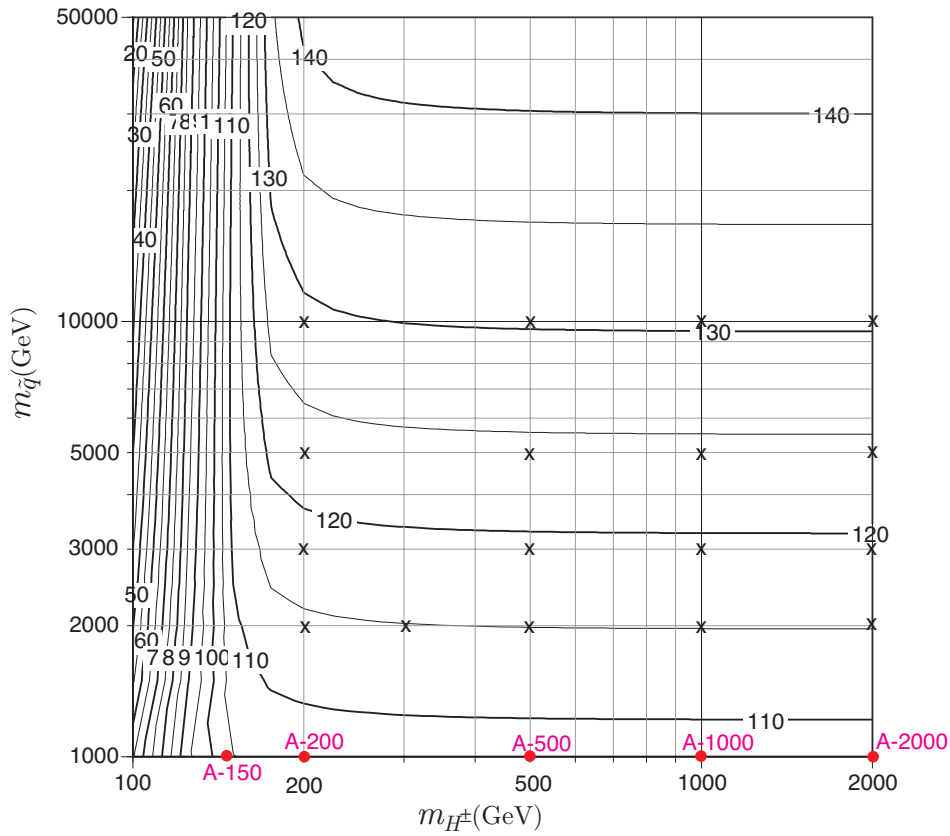
field-dependent mass<sup>2</sup> of the lighter stop:

$$\bar{m}_{\tilde{t}_1}^2 = \frac{1}{2} \left[ m_{\tilde{q}}^2 + m_{\tilde{t}_R}^2 + y_t^2 v_u^2 + \frac{g_2^2 + g_1^2}{4} (v_d^2 - v_u^2) - \sqrt{\left( m_{\tilde{q}}^2 - m_{\tilde{t}_R}^2 + \frac{x_t}{2} (v_d^2 - v_u^2) \right)^2 + y_t^2 |\mu v_d - A_t^* e^{-i\theta} v_u|^2} \right]$$



$$\tan \beta = 10, \mu = 1500\text{GeV}, |A| = 150\text{GeV}$$

mass of the lightest Higgs boson (CP conserving)



## Discussions

**Baryogenesis** requires

1. baryon number violation
2.  $C$  and  $CP$  violation
3. departure from equilibrium



rare<sup>3</sup>

## Electroweak Baryogenesis

- based on a testable model  $\longleftrightarrow$  stringent constraints
- free from proton decay problem

other attempts:

- ★ GUTs
- ★ Leptogenesis
- ★ Affleck-Dine
- ★ Gravitational Baryogenesis  
[Alexander, Peskin & Sheikh-Jabbari, hep-th/0405214]
- ★ Inflationary Baryogenesis [KF, Kakuto, Otsuki & Toyoda, PTP 105]  
[Nanopoulos & Rangarajan, PRD 64]

## viable models for EW baryogenesis

- Minimal SM — excluded !! ✗ {
  - strongly 1st-order EWPT (with acceptable  $m_h$ )
  - sufficient  $CP$  violation
  
- MSSM
  - ★  $m_h \leq 110\text{GeV}$  and  $m_{\tilde{t}_1} \leq m_t$
  - ★  $m_h \leq 120\text{GeV}$  if  $m_{\tilde{t}_R}^2 < 0$ ? }  $\implies$  1st-order EWPT with  $\frac{v_C}{T_C} > 1$
  - ★ many sources of  $CP$  violation
    - complex parameters:  $\mu, M_2, M_1, A; \theta$  —  $\text{Im}(\mu A_t e^{i\theta})$  weakens the EWPT
  
- Other extensions of the MSM
  - ▷ non-SUSY : 2HDM — many parameters not so constrained
  - ▷ Next-to-MSSM (NMSSM) = MSSM + Singlet chiral superfield

## Our recent study of Higgs spectrum and EWPT in the NMSSM

$$W = \epsilon_{ij} \left( y_b H_d^i Q^j B - y_t H_u^i Q^j T + y_l H_d^i L^j E - \lambda N H_d^i H_u^j \right) - \frac{\kappa}{3} N^3$$

$\lambda \langle N \rangle \sim \mu$  in the MSSM

$$\mathcal{L}_{\text{soft}} \ni -m_N^2 n^* n + \left[ \lambda A_\lambda n H_d H_u + \frac{\kappa}{3} A_\kappa n^3 + \text{h.c.} \right].$$

order parameters:  $\langle \Phi_d \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v_{0d} \\ 0 \end{pmatrix}$ ,  $\langle \Phi_u \rangle = \frac{e^{i\theta_0}}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{0u} \end{pmatrix}$ ,  $\langle n \rangle = \frac{e^{i\varphi_0}}{\sqrt{2}} v_{0n}$

tree-level Higgs potential:

$$\begin{aligned} V_0 = & m_1^2 \Phi_d^\dagger \Phi_d + m_2^2 \Phi_u^\dagger \Phi_u + m_N^2 n^* n - \left( \lambda A_\lambda \epsilon_{ij} n \Phi_d^i \Phi_u^j + \frac{\kappa}{3} A_\kappa n^3 + \text{h.c.} \right) \\ & + \frac{g_2^2 + g_1^2}{8} \left( \Phi_d^\dagger \Phi_d - \Phi_u^\dagger \Phi_u \right)^2 + \frac{g_2^2}{2} \left| \Phi_d^\dagger \Phi_u \right|^2 \\ & + |\lambda|^2 n^* n \left( \Phi_d^\dagger \Phi_d + \Phi_u^\dagger \Phi_u \right) + \left| \lambda \epsilon_{ij} \Phi_d^i \Phi_u^j + \kappa n^2 \right|^2 \end{aligned}$$

1. 5 neutral and 1 charged scalars (3 scalar and 2 pseudoscalar when CP cons.)

The lightest Higgs scalar can escape from the lower bound 114GeV, because of small coupling to  $Z$  caused by large mixing among 3 scalars. [Miller, et al. NPB 681]

— “Light Higgs Scenario” —

2. CP violation at the tree level:  $\text{Im}(\lambda A_\lambda e^{i(\theta+\varphi)})$ ,  $\text{Im}(\kappa A_\kappa e^{3i\varphi})$ ,  $\text{Im}(\lambda \kappa^* e^{i(\theta-2\varphi)})$

3.  $v_n \rightarrow \infty$  with  $\lambda v_n$  and  $\kappa v_n$  fixed  $\implies$  MSSM [Ellis, et al, PRD 39]

$\longrightarrow$  new features expected for  $v_n = O(100)\text{GeV}$

---

- ★ study of the Higgs spectrum and couplings without/with CP violation  $\Leftarrow$

[KF and Tao, hep-ph/0409294]

- ★ study of the EWPT without/with CP violation  $\Leftarrow$  preliminary

- ★ sphaleron solution

[KF, et al. in progress]

many parameters in the model

— in the Higgs sector, soft masses,  $\lambda, \kappa, A_\lambda, A_\kappa$   
*complex parameters*

$$\begin{aligned}
 R_\lambda &= \frac{1}{\sqrt{2}} \operatorname{Re} \left( \lambda A_\lambda e^{i(\theta_0 + \varphi_0)} \right), & I_\lambda &= \frac{1}{\sqrt{2}} \operatorname{Im} \left( \lambda A_\lambda e^{i(\theta_0 + \varphi_0)} \right), \\
 R_\kappa &= \frac{1}{\sqrt{2}} \operatorname{Re} \left( \kappa A_\kappa e^{3i\varphi_0} \right), & I_\kappa &= \frac{1}{\sqrt{2}} \operatorname{Im} \left( \kappa A_\kappa e^{3i\varphi_0} \right), \\
 \mathcal{R} &= \operatorname{Re} \left( \lambda \kappa^* e^{i(\theta_0 - 2\varphi_0)} \right), & \mathcal{I} &= \operatorname{Im} \left( \lambda \kappa^* e^{i(\theta_0 - 2\varphi_0)} \right)
 \end{aligned}$$

“tadpole condition”:  $\left\langle \frac{\partial V_{\text{eff}}}{\partial h_i} \right\rangle = \left\langle \frac{\partial V_{\text{eff}}}{\partial a_i} \right\rangle = 0$

$$m_1^2 = \left( R_\lambda - \frac{1}{2} \mathcal{R} v_{0n} \right) v_{0n} \tan \beta_0 - \frac{1}{2} m_Z^2 \cos(2\beta_0) - \frac{|\lambda|^2}{2} (v_{0n}^2 + v_{0u}^2) + \dots$$

...

$$m_N^2 = (R_\lambda - \mathcal{R} v_{0n}) \frac{v_{0d} v_{0u}}{v_{0n}} + R_\kappa v_{0n} - \frac{|\lambda|^2}{2} (v_{0d}^2 + v_{0u}^2) - |\kappa|^2 v_{0n}^2 + \dots$$

$$I_\lambda = \frac{1}{2} \mathcal{I} v_{0n} + \dots, \quad I_\kappa = -\frac{3}{2} \mathcal{I} \frac{v_{0d} v_{0u}}{v_{0n}}$$

mass matrix of the neutral Higgs bosons

$$\mathcal{M}^2 \equiv \begin{pmatrix} \left\langle \frac{\partial^2 V_{\text{eff}}}{\partial h_i \partial h_j} \right\rangle & \left\langle \frac{\partial^2 V_{\text{eff}}}{\partial h_i \partial a_j} \right\rangle \\ \left\langle \frac{\partial^2 V_{\text{eff}}}{\partial a_i \partial h_j} \right\rangle & \left\langle \frac{\partial^2 V_{\text{eff}}}{\partial a_i \partial a_j} \right\rangle \end{pmatrix} \xrightarrow{\text{extract NG modes}} \begin{pmatrix} \mathcal{M}_S^2 & \mathcal{M}_{SP}^2 \\ \mathcal{M}_{SP}^{2T} & \mathcal{M}_P^2 \end{pmatrix}$$

$$\mathcal{M}_{SP}^2 \propto \mathcal{I}$$

We use  $m_{H^\pm}$  as an input, instead of  $R_\lambda$ :

$$m_{H^\pm}^2 = \frac{1}{\sin \beta \cos \beta} \left\langle \frac{\partial^2 V_{\text{eff}}}{\partial \phi_d^+ \partial \phi_u^-} \right\rangle = m_W^2 - \frac{1}{2} |\lambda|^2 v^2 + (2R_\lambda - \mathcal{R} v_{0n}) \frac{v_{0n}}{\sin 2\beta_0} + \dots$$



## Definition of the couplings

gauge vs mass eigenstates: 
$$\begin{pmatrix} h_d \\ h_u \\ h_n \\ a \\ a_n \end{pmatrix} = \mathcal{O} \begin{pmatrix} H_1 \\ H_2 \\ H_3 \\ H_4 \\ H_5 \end{pmatrix}, \quad \mathcal{O}^T \mathcal{M}^2 \mathcal{O} = \text{diag}(m_{H_1}^2, \dots, m_{H_5}^2)$$

$$\mathcal{L}_{\text{gauge}} \ni g_2 m_W g_{VVH_i} \left( W_\mu^+ W^{-\mu} + \frac{1}{2 \cos^2 \theta_W} Z_\mu Z^\mu \right) H_i + \frac{g_2}{2 \cos \theta_W} g_{ZH_iH_j} Z^\mu (H_i \overleftrightarrow{\partial}_\mu H_j)$$

$$\mathcal{L}_Y \ni -\frac{g_2 m_b}{2 m_W} \bar{b} (g_{bbH_i}^S + i \gamma^5 g_{bbH_i}^P) b H_i$$

$$\left\{ \begin{array}{l} g_{VVH_i} = \mathcal{O}_{1i} \cos \beta + \mathcal{O}_{2i} \sin \beta \\ g_{ZH_iH_j} = \frac{1}{2} \{ (\mathcal{O}_{4i} \mathcal{O}_{2j} - \mathcal{O}_{4j} \mathcal{O}_{2i}) \cos \beta - (\mathcal{O}_{4i} \mathcal{O}_{1j} - \mathcal{O}_{4j} \mathcal{O}_{1i}) \sin \beta \} \\ g_{bbH_i}^S = \mathcal{O}_{1i} \frac{1}{\cos \beta}, \quad g_{bbH_i}^P = -\mathcal{O}_{4i} \tan \beta \\ g_{bbH_i}^2 \equiv (g_{bbH_i}^S)^2 + (g_{bbH_i}^P)^2 \end{array} \right.$$

inputs:

$$v_0 = 246\text{GeV}, \tan \beta_0, v_{0n}, m_{H^\pm}, |\lambda|, |\kappa|, |A_\lambda|, |A_\kappa|, \text{Arg}\kappa \quad [m_{\tilde{q}}, m_{\tilde{t}_R} = m_{\tilde{b}_R}, A_t]$$

some combination of the phases is constrained

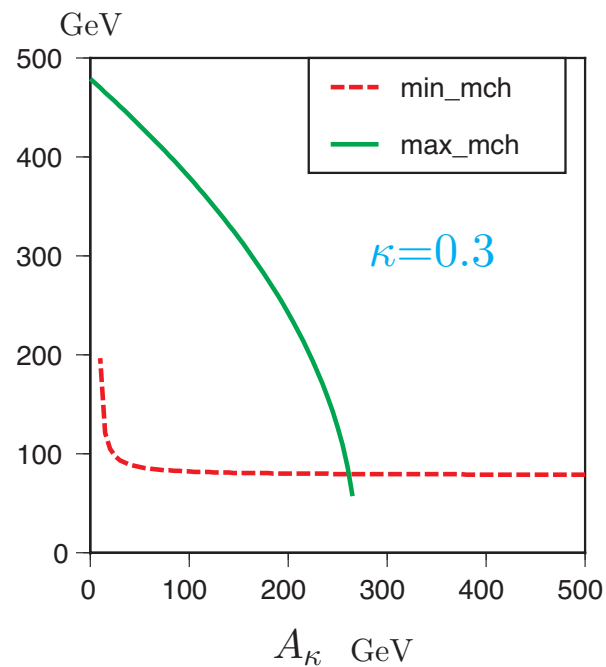
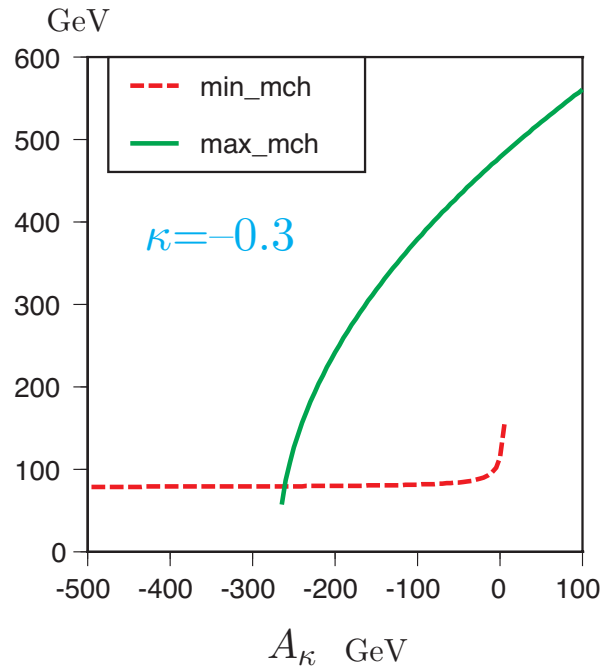
- We require** {
1. all the mass<sup>2</sup> of the scalars  $> 0$
  2.  $m_{H_i} > 114\text{GeV}$  or  $g_{H_i ZZ}^2 < 0.01$  spectrum condition
  3.  $V_{\text{eff}}(\mathbf{0}) > V_{\text{eff}}(\mathbf{v}_0)$  vacuum condition-0
  4. no global mim. of  $V_{\text{eff}}$  other than  $\mathbf{v}_0$  vacuum condition

condition-1  $\ni \det \mathcal{M}_P^2 > 0 \Rightarrow$  lower bound on  $m_{H^\pm}$  [cf,  $m_{H^\pm}$  vs  $m_A$  in the MSSM]

condition-3 at the tree level

$$m_{H^\pm}^2 < m_W^2 + m_Z^2 \cot^2 2\beta_0 + \frac{2|\lambda|^2 v_{0n}^2}{\sin^2 2\beta_0} + \frac{2|\kappa|^2 v_{0n}^4}{v_0^2 \sin^2 2\beta_0} + \frac{\mathcal{R} v_{0n}^2}{\sin 2\beta_0} - \frac{4R_\kappa v_{0n}^3}{3v_0^2 \sin^2 2\beta_0}$$

$\tan\beta = 5, v_n = 300\text{GeV}$

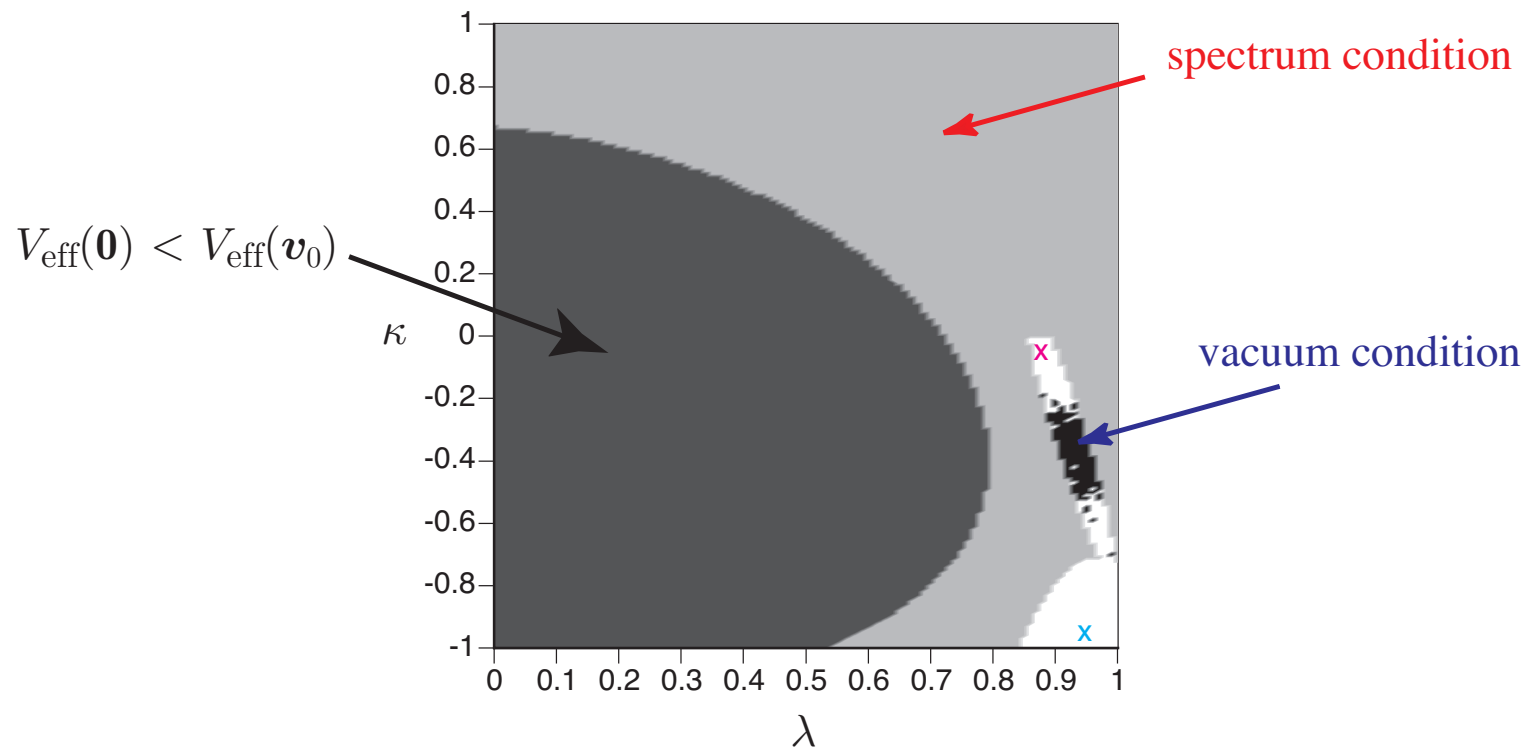


$\Rightarrow \kappa A_k > 0$  is favored

## numerical search for allowed parameter region

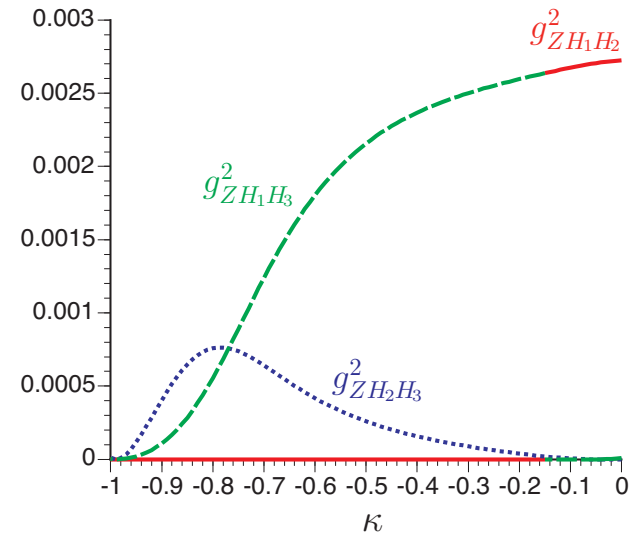
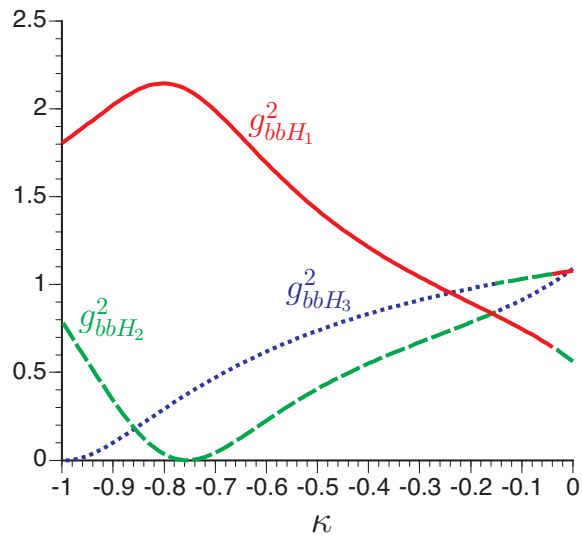
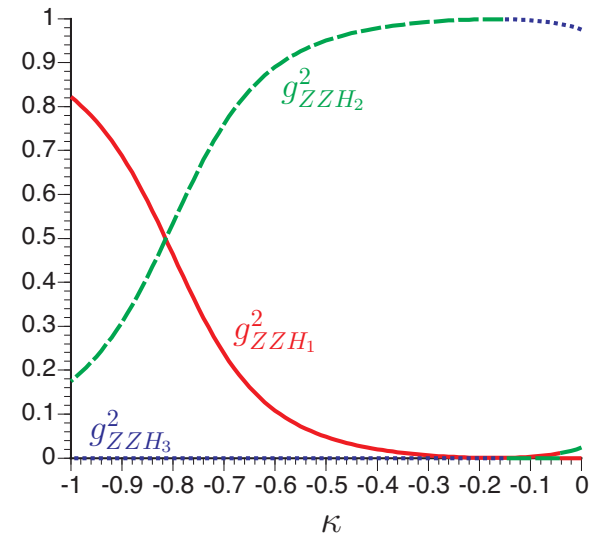
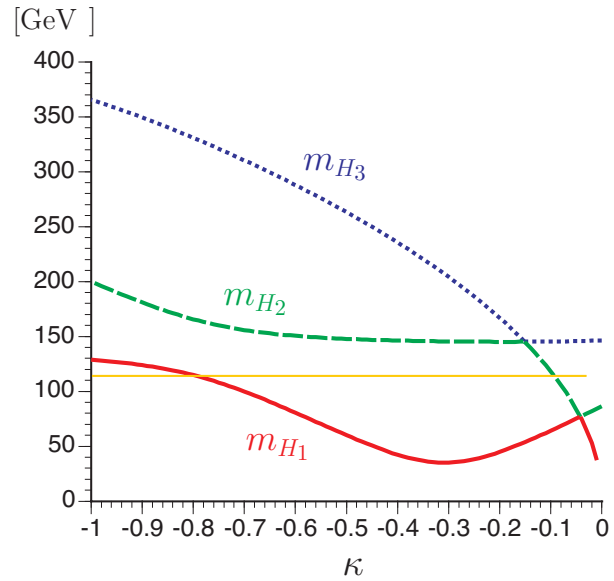
$\tan \beta_0 = 3 - 20$ ,  $v_{0n} = 100 - 1000 \text{ GeV}$ ,  $m_{H^\pm} = 100 - 5000 \text{ GeV}$ ,  $-A_\kappa = 0 - 1000 \text{ GeV}$

*e.g.*,  $\tan \beta_0 = 3$ ,  $v_{0n} = 200 \text{ GeV}$ ,  $m_{H^\pm} = 400 \text{ GeV}$ ,  $A_\kappa = -200 \text{ GeV}$ , heavy squark



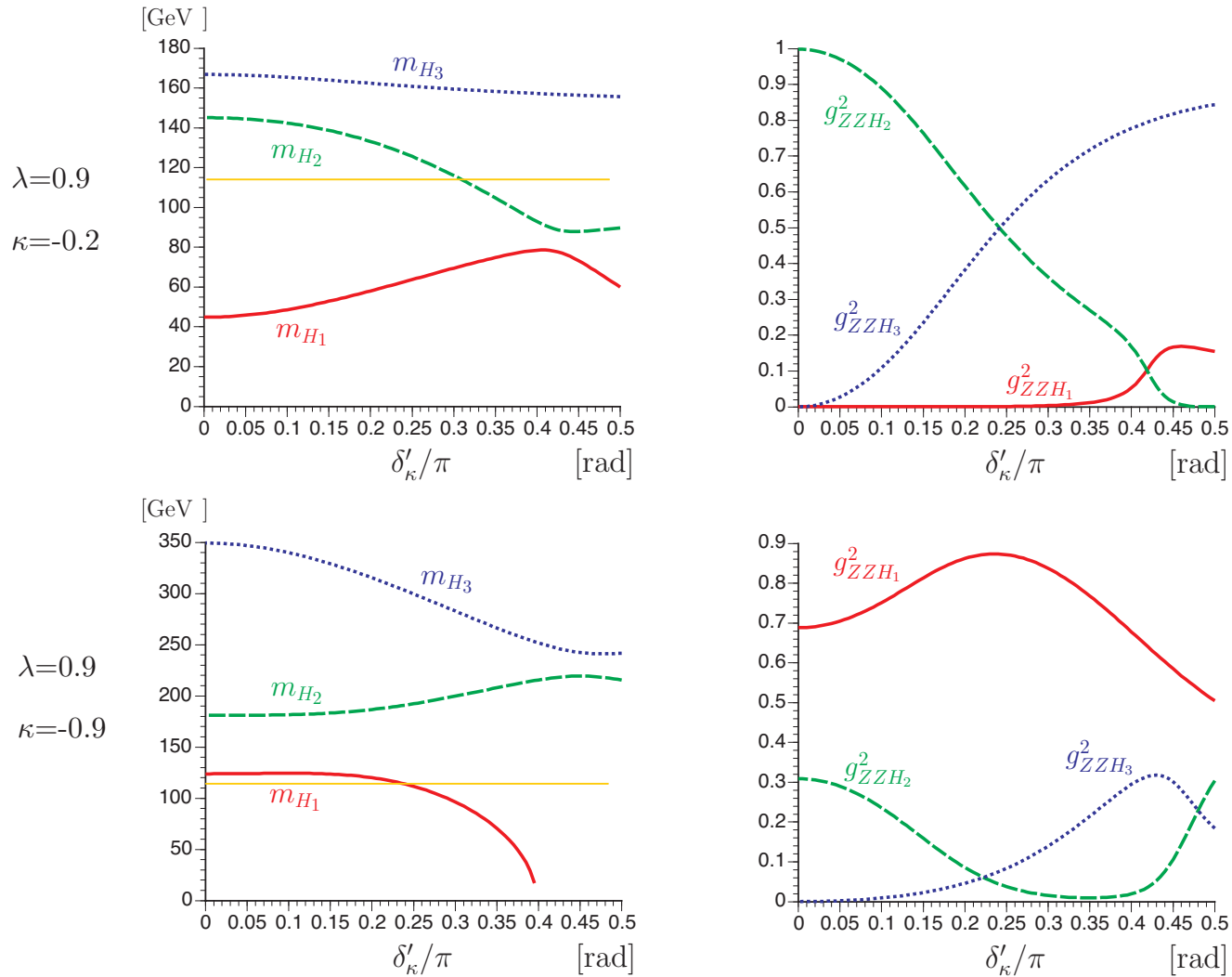
$\lambda$	$\kappa$	$m_{H_1}$	$m_{H_2}$	$m_{H_3}$	$m_{H_4}$	$m_{H_5}$	$g_{H_1 ZZ}^2$	$g_{H_2 ZZ}^2$	$g_{H_3 ZZ}^2$	$g_{H_4 ZZ}^2$	$g_{H_5 ZZ}^2$
0.9	-0.05	75.0	83.5	145.7	436.0	448.2	0.0094	0	0.9897	0.0009	0
0.95	-0.95	139.6	180.9	360.3	425.4	456.4	0.828	0.170	0	0	0.0028

along the line of  $\lambda = 0.9$ ,



# Effects of CP violation

$$\delta'_\kappa \equiv \text{Arg}\kappa + 3\varphi_0 \quad \text{Arg}\lambda + \theta_0 + \varphi_0 = 0 \Leftrightarrow \text{small EDM}$$



[MSSM with nonzero  $\text{Im}(\mu A_q e^{i\theta_0})$  : Carena, et al. NPB586]

# EWPT [preliminary]

naive (?) argument

[Pietroni, NPB402]

$$\text{order parameters : } \begin{cases} v_d = v \cos \beta(T) = y \cos \alpha(T) \cos \beta(T), \\ v_u = v \sin \beta(T) = y \cos \alpha(T) \sin \beta(T), \\ v_n = y \sin \alpha(T) \end{cases}$$

$$V_0 = \frac{1}{2} \left( (m_1^2 \cos^2 \beta + m_2^2 \sin^2 \beta) \cos^2 \alpha + m_N^2 \sin^2 \alpha \right) y^2 \\ - \left( R_\lambda \cos^2 \alpha \sin \alpha \cos \beta \sin \beta + \frac{1}{3} R_\kappa \sin^3 \alpha \right) y^3 + \dots$$

strongly 1st order PT by the tree-level cubic term

Is such a parametrization valid ?

— no symmetry between the doublets and the singlet

## 2-stage Phase Transition

$T_C \equiv$  PT temperature of the EWPT *i.e.*, at which  $v = \sqrt{v_d^2 + v_u^2} \rightarrow 0$

$T_N \equiv$  PT temperature at which  $v_n \rightarrow 0$

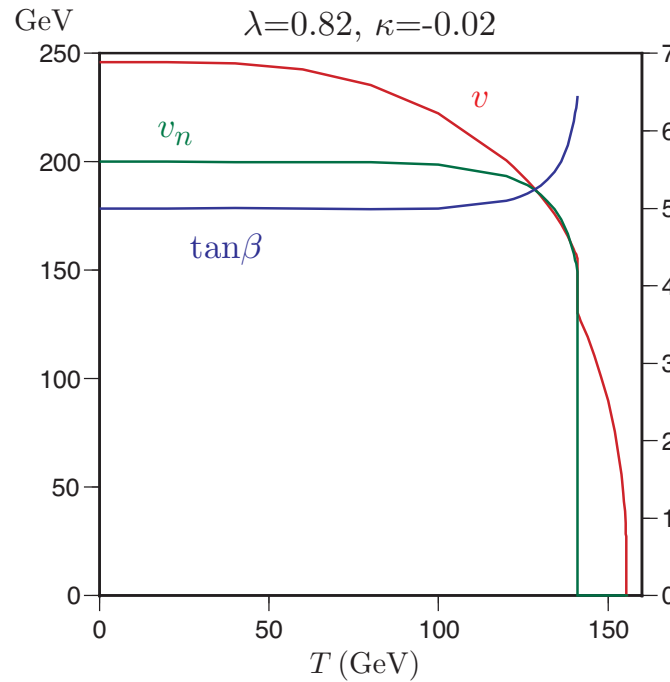
- (1)  $T_C > T_N$  — first-order EWPT requires a light stop  
for  $T_N < T < T_C$ ,  $\exists U(1)$  symmetry of the singlet
- (2)  $T_C = T_N$  — strongly first order
- (3)  $T_C < T_N$  — MSSM-like EWPT

roughly speaking,  $\left\{ \begin{array}{ll} \text{light Higgs} & \implies (1), (2) \\ \text{heavy Higgs} & \implies (3) \end{array} \right.$



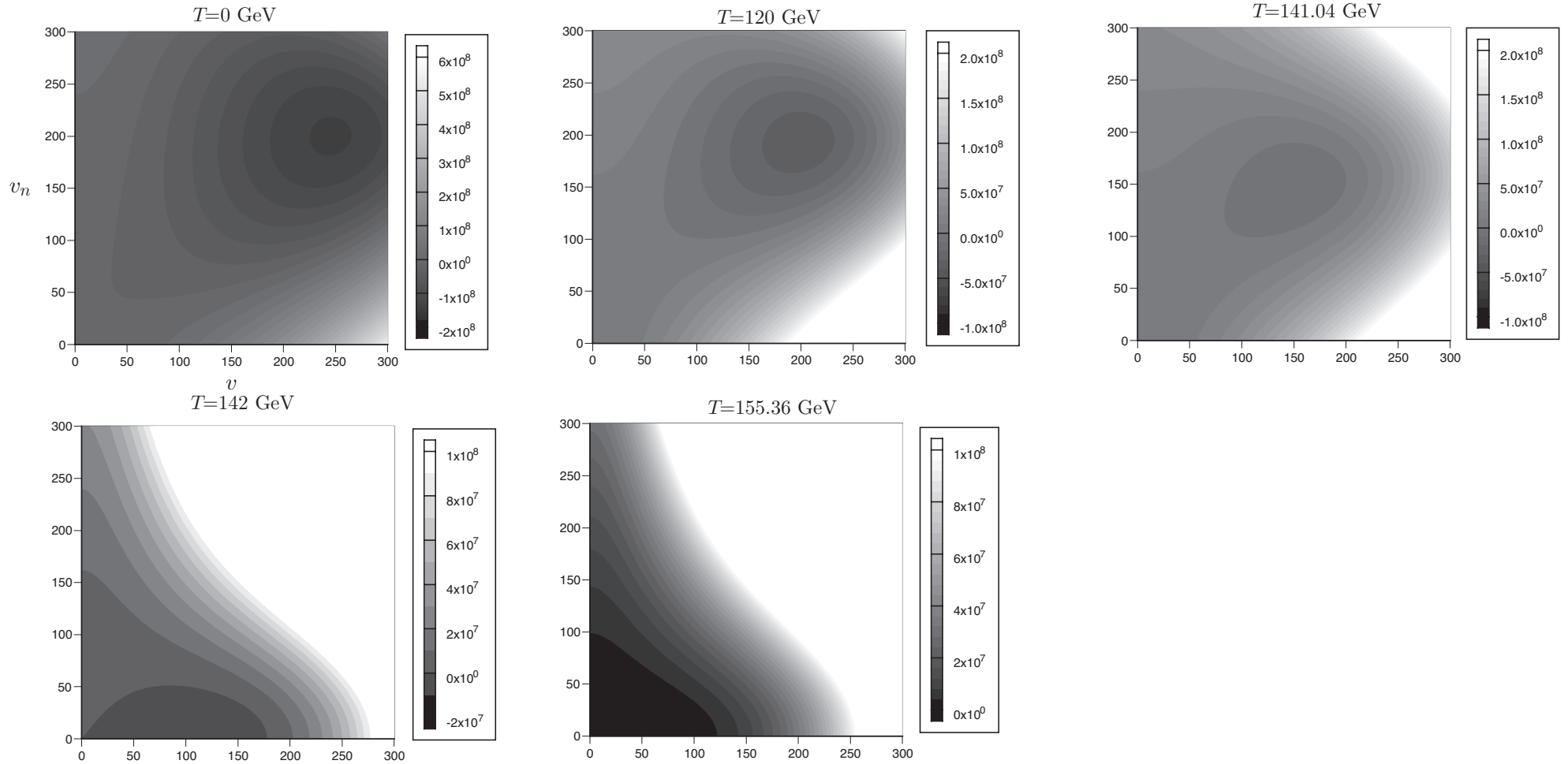
## Ex-1 (light Higgs)

$\tan \beta = 5$ ,  $m_{H^\pm} = 600\text{GeV}$ ,  $A_\kappa = -100\text{GeV}$ ,  $\lambda = 0.82$ ,  $\kappa = -0.02$ , heavy squark



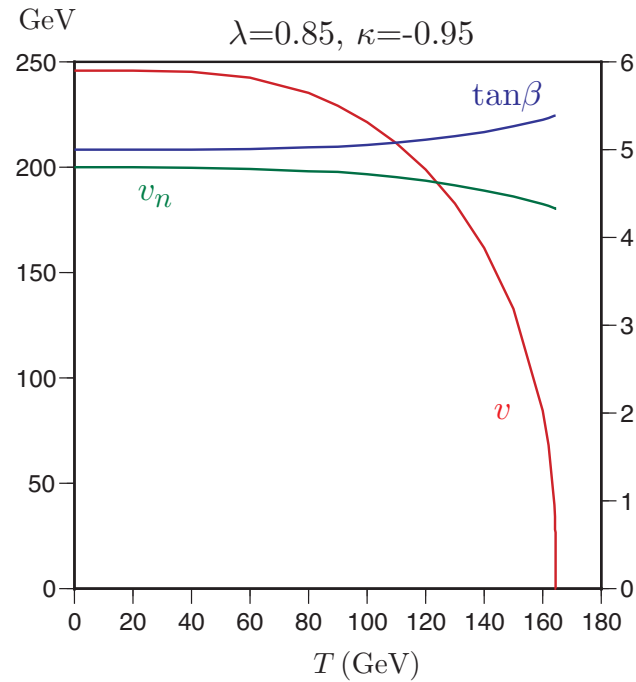
$$\begin{aligned}
 (v_d, v_u, v_n) &= (48.2, 241.2, 200) \rightarrow (23.8, 153.3, 149.0) \xrightarrow{T_N=126.8\text{GeV}} (0, 130.2, 0) \\
 &\rightarrow (0, 26.0, 0) \xrightarrow{T_C=155.4\text{GeV}} (0, 0, 0)
 \end{aligned}$$

reduced effective potential:  $\tilde{V}_{\text{eff}}(v, v_n; T) \equiv V_{\text{eff}}(v \cos \beta(T), v \sin \beta(T), v_n; T)$



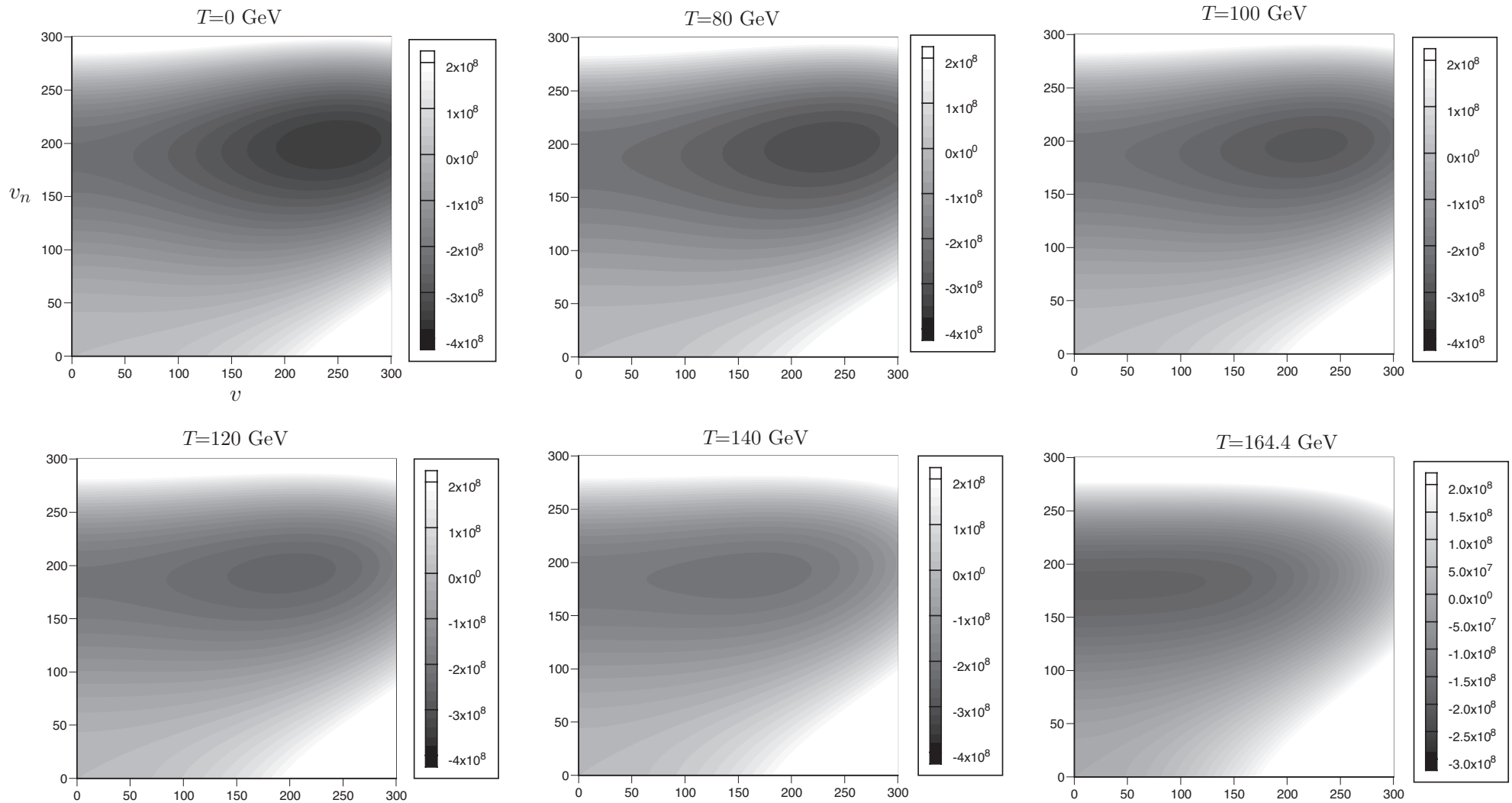
## Ex-2 (heavy Higgs)

$\tan \beta = 5$ ,  $m_{H^\pm} = 600\text{GeV}$ ,  $A_\kappa = -100\text{GeV}$ ,  $\lambda = 0.85$ ,  $\kappa = -0.95$ , heavy squark



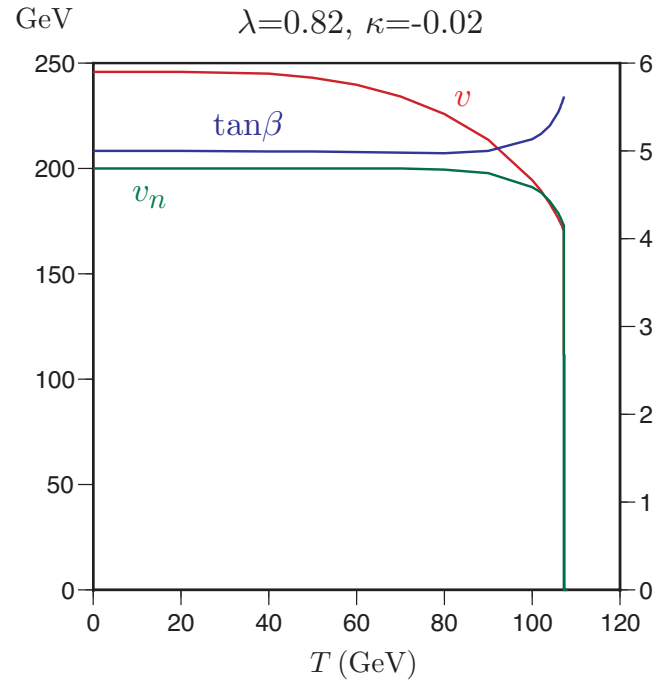
$$(v_d, v_u, v_n) = (48.2, 241.2, 200) \rightarrow (4.9, 26.4, 180.5) \xrightarrow{T_C=164.36\text{GeV}} (0, 0, 180.4)$$

$$T_N \gg 200\text{GeV}$$



### Ex-3 (light Higgs)

the same parameters as Ex-1, except for  $m_{\tilde{t}_R} = 800\text{GeV} \rightarrow 10\text{GeV}$  (light squark)



$$\begin{aligned}
 (v_d, v_u, v_n) &= (48.2, 241.2, 200) \rightarrow (29.8, 167.8, 172.6) \xrightarrow{T_N=107.28\text{GeV}} (0, 111.7, 0) \\
 &\rightarrow (0, 110.2, 0) \xrightarrow{T_C=107.40\text{GeV}} (0, 0, 0)
 \end{aligned}$$

for a lighter squark,  $T_C \rightarrow T_N$  and stronger PT

works in progress

- Phase transition in the presence of CP violation  
CP violation not affecting the EDM
- Sphaleron solution for various boundary conditions  
 $v_n = 0$  and  $v_n \neq 0$  in the broken phase ( $v \neq 0$ )

to-do

- ★ CP violation in the phase boundary
- ★ Calculation of the generated baryon number
  - \* formalism: quantum and semi-classical — CTP ?
  - \* space-varying  $\text{Im}\mu \sim \text{Im}\langle N \rangle \neq 0$ 
    - ⇒ quark/lepton, chargino/neutralino, squark/slepton